Solution (#1711) If we apply the Laplace transform then we find

$$\bar{f}(s) = \frac{2}{(s-1)^2} + \frac{1}{s+1}$$

which is the Laplace transform of

$$f(x) = 2xe^x + e^{-x}.$$