**Solution** (#238) With an appropriate inductive hypothesis make use of the identity

$$2\cos\frac{\pi}{2^{n+2}} = \sqrt{2 + 2\cos\frac{\pi}{2^{n+1}}}.$$