**Solution** (#345) By a careful induction involving  $F_{3n}$ ,  $F_{3n+1}$ ,  $F_{3n+2}$  show that  $F_{3n}$  is even,  $F_{3n+1}$  is odd,  $F_{3n+2}$  is odd.