

Solution (#1390) Split the integral into two intervals, $(0, 1)$ and $(1, \infty)$ and set $u = 1/x$ in the second integral.

This same method would work to show

$$\int_0^\infty \frac{f(x - x^{-1})}{x} dx = 0$$

for any odd function $f(x)$.