Solution (#1032) Let M denote the transition matrix for the Sunny/Rainy model in #606. We defined

$$M = \left(\begin{array}{cc} 0.9 & 0.1\\ 0.5 & 0.5 \end{array}\right).$$

 So

$$M^{2} = \begin{pmatrix} 0.86 & 0.14 \\ 0.7 & 0.3 \end{pmatrix}, \qquad M^{3} = \begin{pmatrix} 0.844 & 0.156 \\ 0.78 & 0.22 \end{pmatrix}.$$

The probability that it is Sunny on Day 3 given it is Rainy on Day 0 equals 0.78. The probability that it is Sunny on Day 11 given it is Sunny on Day 8 equals 0.844 as the transition matrix from Day 8 to Day 11 is the same as the transition matrix from Day 0 to Day 3.

In #407 we worked out the long term chance of sun as 5/6 and of rain as 1/6. Hence for large n we have

$$M^n \approx \left(\begin{array}{cc} 5/6 & 1/6\\ 5/6 & 1/6 \end{array}\right)$$

This is saying that the long-term forecast is largely independent of the weather on Day 0.