

Sharpening previous results of Baldwin and Shelah [2,11], the authors prove some equivalences to monadic NIP. In particular, they prove that the following are equivalent for a complete theory  $T$  with infinite models (see the paper for precise definitions):

- (1)  $T$  is monadically NIP, i.e. every expansion by unary predicates is NIP;
- (2) No monadic expansion of  $T$  admits coding of pairs of singletons by singletons;
- (3)  $T$  does not admit coding of pairs of tuples by singletons;
- (4)  $T$  has the *f.s. dichotomy*: if  $\text{tp}(b/Ma)$  is finitely satisfiable in  $M \models T$ , then for any singleton  $c$ , either  $\text{tp}(b/Mac)$  or  $\text{tp}(bc/Ma)$  is finitely satisfiable in  $M$ ;
- (5) If  $M, N \models T$  then any  $M$ -*f.s. decomposition* of any subset of  $N$ , meaning a decomposition into a sequence of chunks  $A_i$  with  $\text{tp}(A_i/M A_{<i})$  finitely satisfiable in  $M$ , extends (in a certain sense) to such a decomposition of  $N$ ;
- (6)  $T$  is dp-minimal and has *indiscernable-triviality*, i.e. indiscernability over  $B$  is equivalent to indiscernability over each singleton  $b \in B$ .

They deduce that if  $T$  has quantifier elimination in a relational language with finitely many constants, then  $T$  is monadically NIP iff  $\text{Age}(T)$  is NIP, and they obtain a lower bound on the growth rate of  $\text{Age}(T)$  when  $T$  is not monadically NIP.