

Upstream Forcing of Tidewater Glacier Retreat

Ian Hewitt, University of Oxford

- Tidewater glaciers currently discharge around half of Greenland's ice loss to the ocean, and can change rapidly.
- Central question: **what controls ice discharge?** and, related to that, **what determines the location of the ice front?**

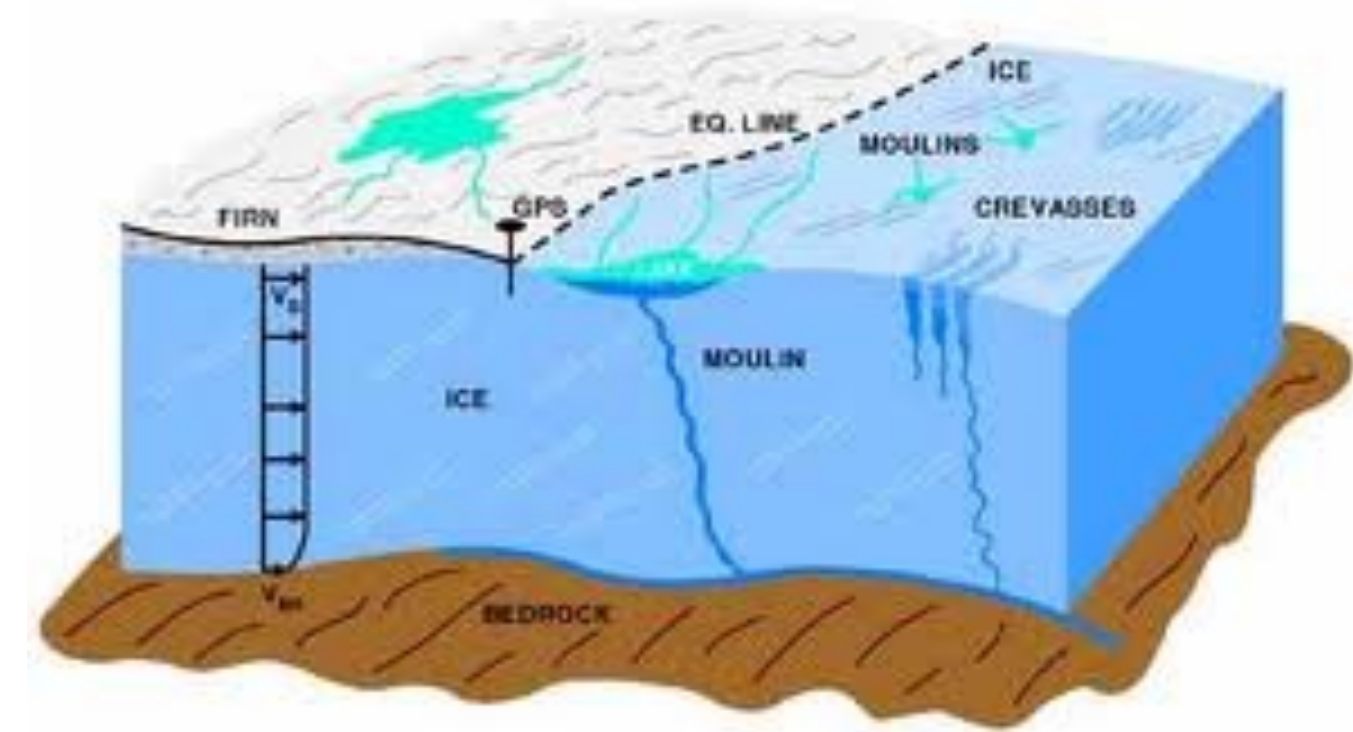
Summary

- Certain positions of the ice front act as '**pinning points**', at which the glacier achieves a roughly steady balance (accumulation \approx discharge).
Changes in forcing can cause such points to disappear or lose stability.
- The highly non-linear response is inherent to the dynamics of tidewater glaciers, whether forcing is **from the ocean or from upstream**.
- I'll describe a simplified model that helps elucidate this.



Motivation: impact of subglacial lubrication

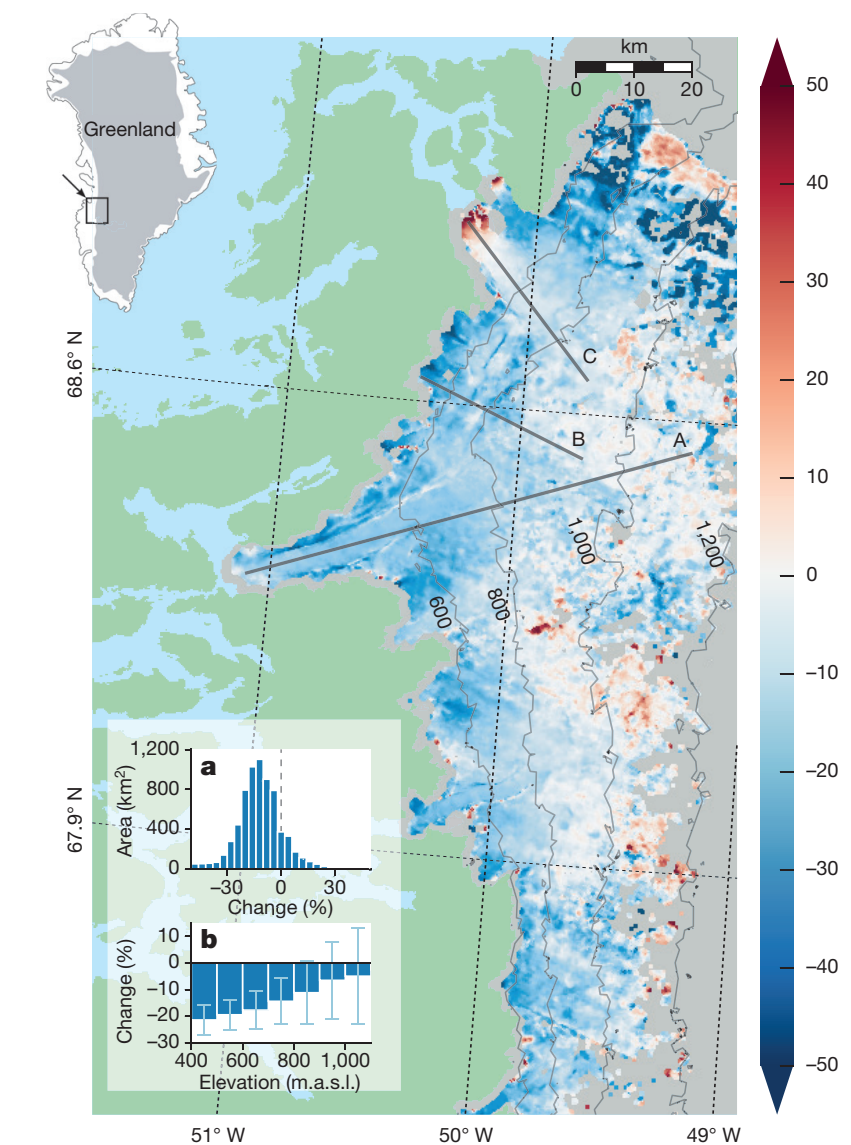
- Drainage of **surface meltwater** to the bed affects **ice speed** (due to influence on water pressure).
- Possibility that increased surface melt could cause increased ice speeds, and consequently (perhaps?) ice loss.



Zwally et al 2002

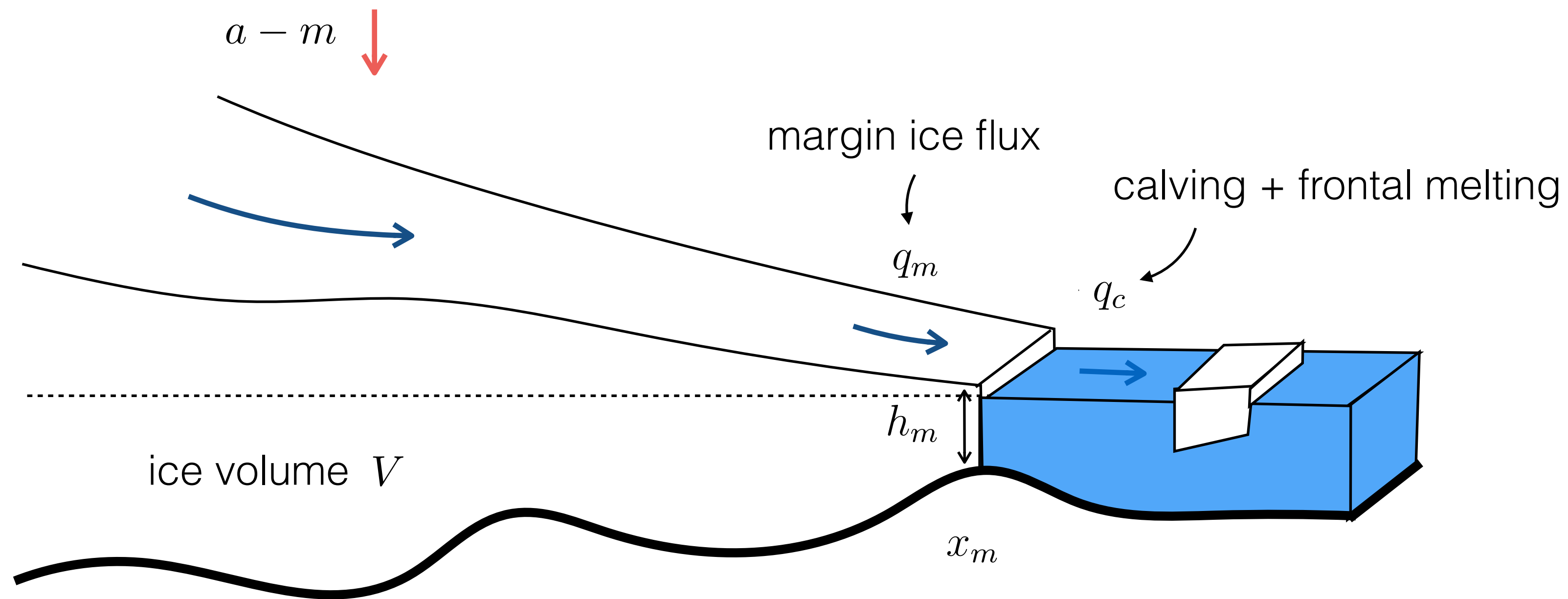
- Some recent studies suggest increased surface melt may have caused a slight **decrease** in average ice speeds (due to more efficient subglacial drainage).

➔ **What impact do we expect such changes to have on a tidewater glacier?**



Tedstone et al 2015

Ice front evolution

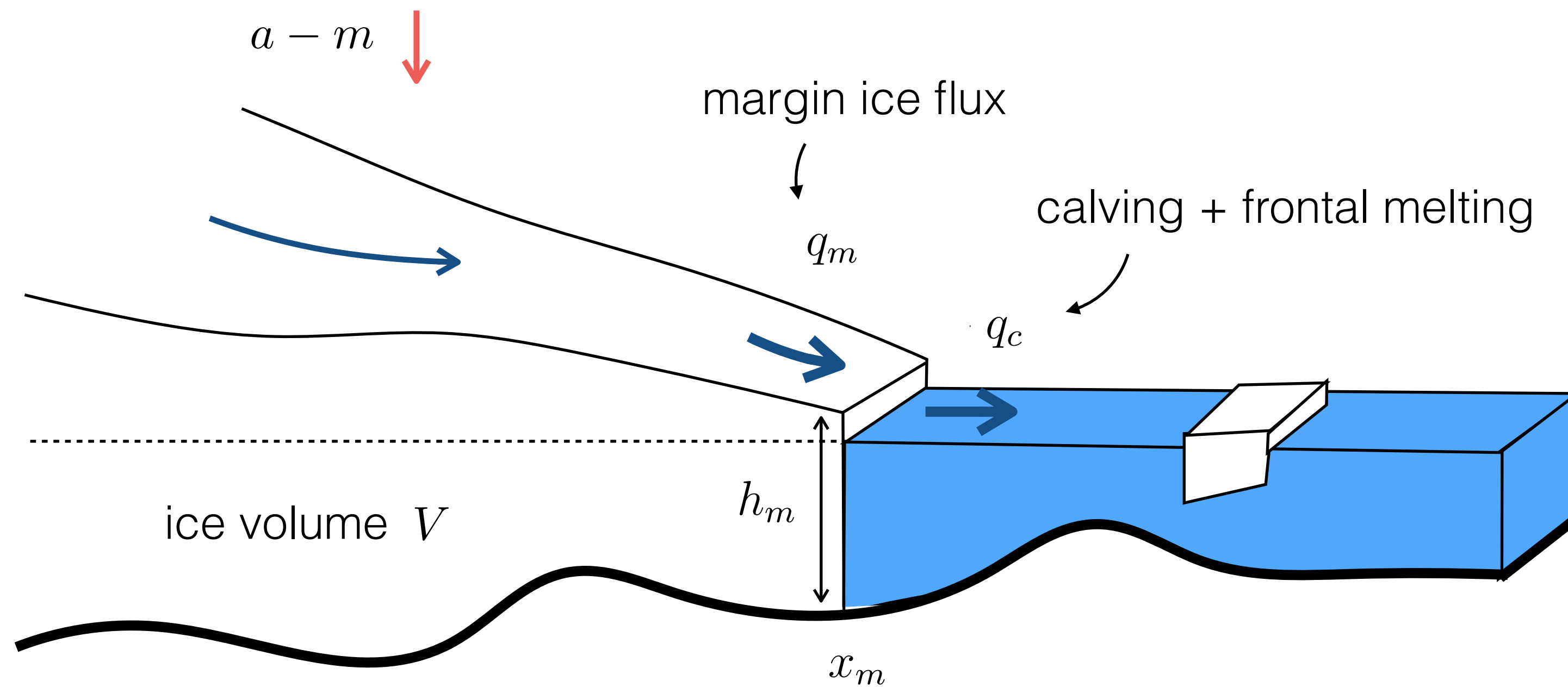


Kinematic condition

$$h_m \frac{dx_m}{dt} = q_m - q_c$$

- Primary control on discharge is ice **depth** at the margin.
- It is typically observed that $q_m \approx q_c$

Ice front evolution

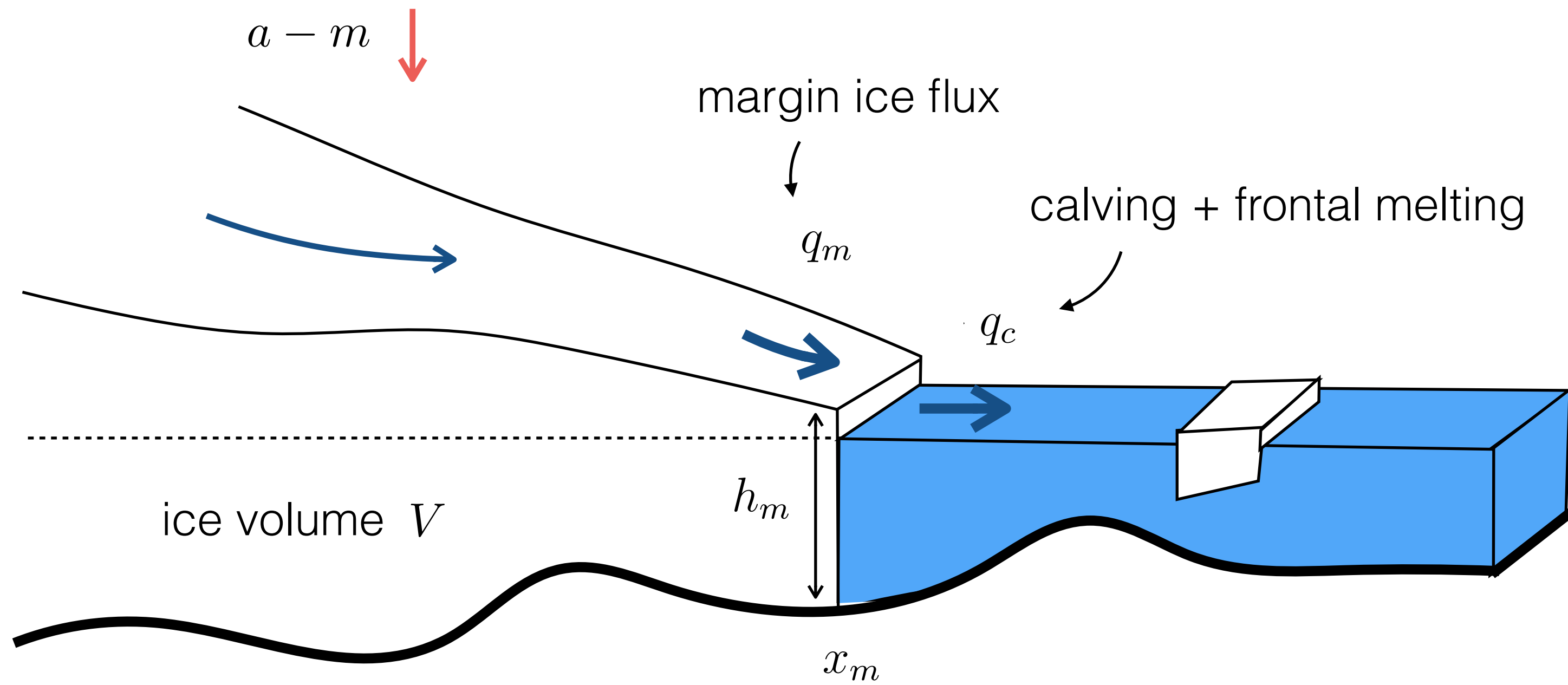


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Global mass balance

$$\frac{dV}{dt} = q_b - q_c$$

balance flux $q_b = \int_0^{x_m} (a - m) dx$

Time-lapse movie



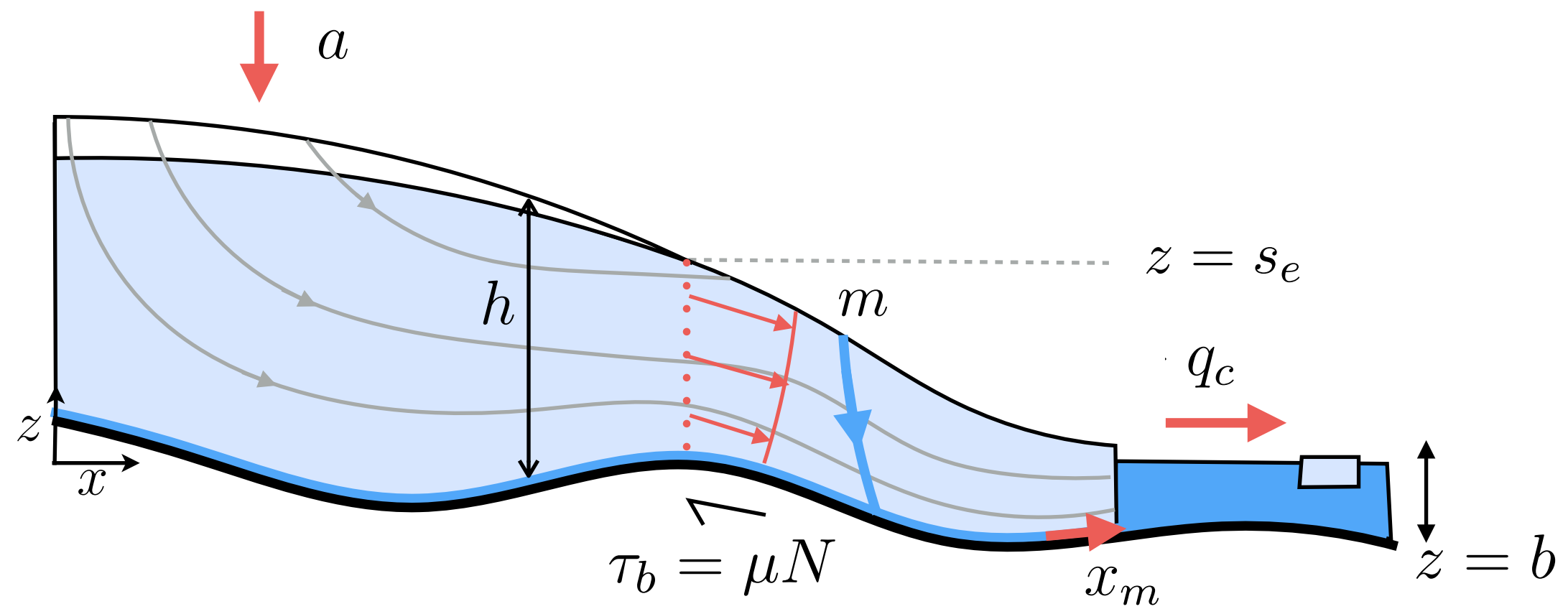
Extreme Ice Survey - Time-lapse camera
Columbia Glacier, Alaska

Time-lapse movie



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A simplified model of a tidewater glacier



Two-dimensional. Ice motion dominated by basal sliding.
 A **plastic** (rate-independent) friction law.

Mass conservation $\frac{\partial h}{\partial t} + \frac{\partial q}{\partial x} = a - m$ $q = hu$

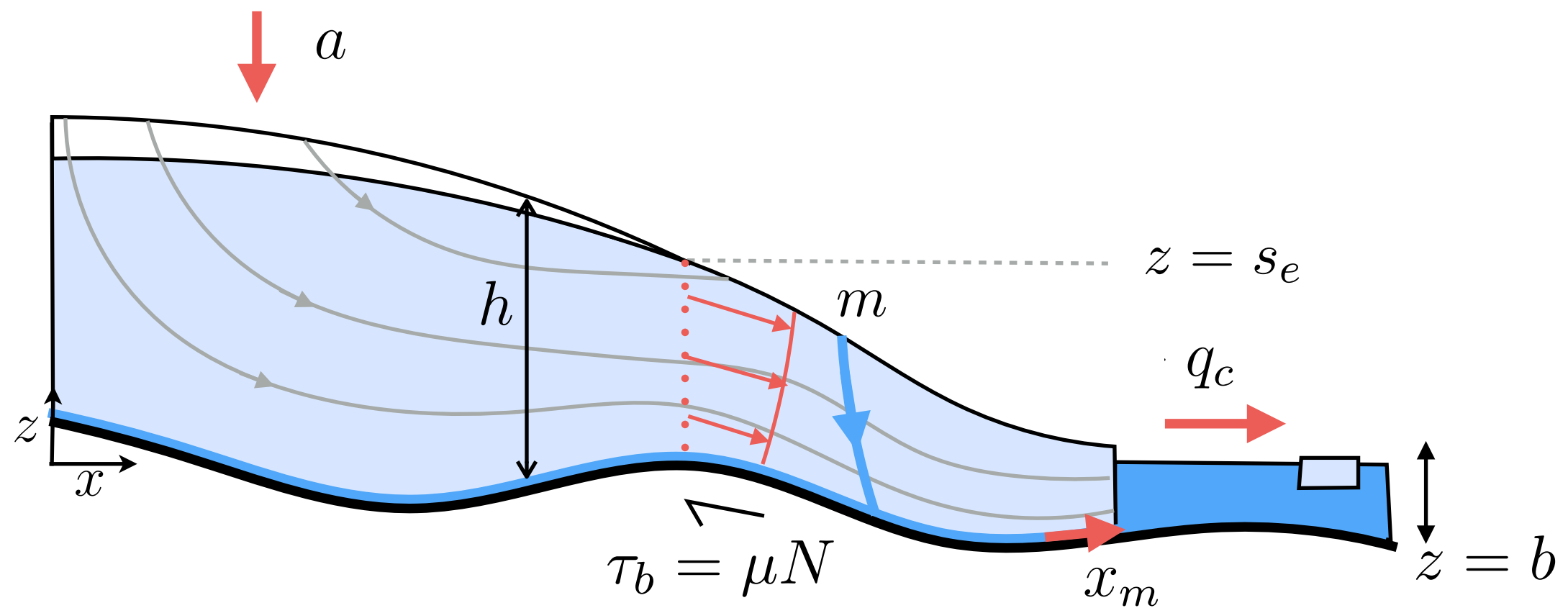
Force balance $\frac{\partial}{\partial x} \left(4\eta_i h \frac{\partial u}{\partial x} \right) - \rho_i g h \frac{\partial}{\partial x} (b + h) - \tau_b = 0$

At ice front $x = x_m$ $4\eta_i h \frac{\partial u}{\partial x} = \frac{1}{2} (\rho_i g h^2 - \rho_o g b^2)$ (stress balance)

$h = f \left(-\frac{\rho_o}{\rho_i} b \right)$ (calving criteria)

flotation factor \uparrow $\left(-\frac{\rho_o}{\rho_i} b \right)$ \leftarrow flotation depth

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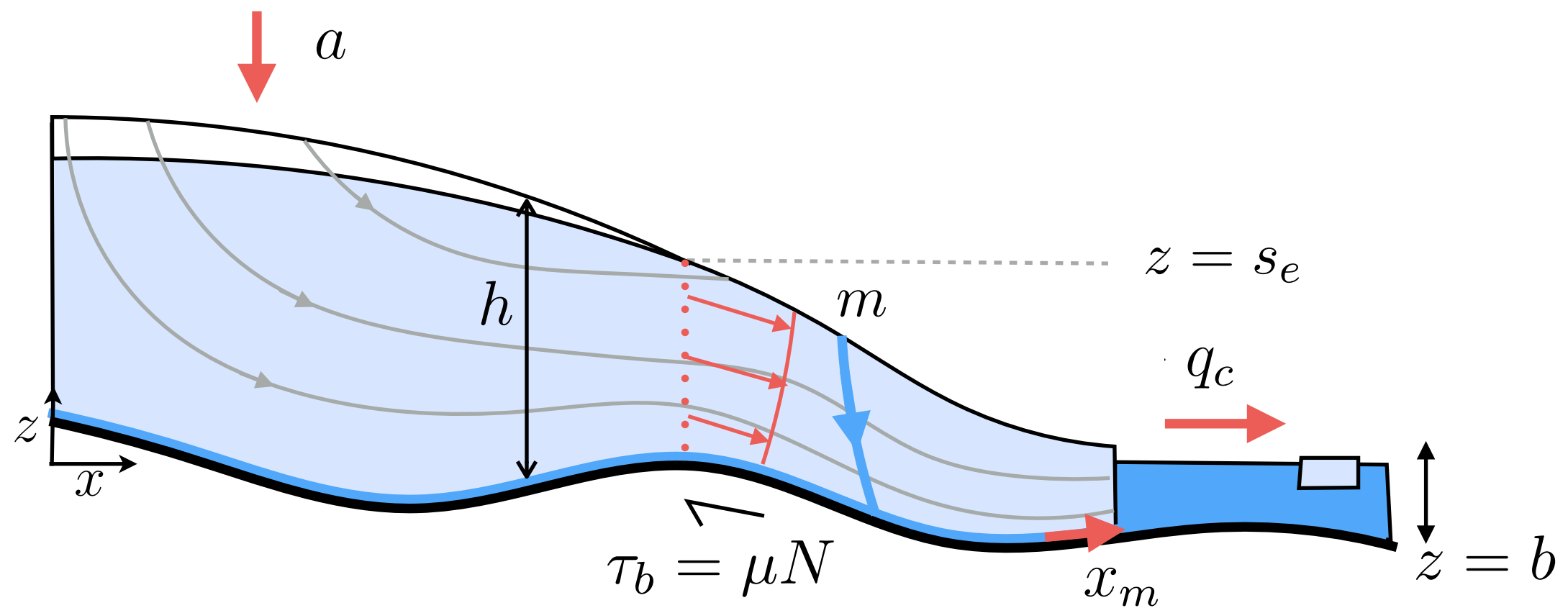


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	↑ flotation factor	↑ flotation depth

- Model reduction**
- Away from the front, force balance $-\rho_i g h \frac{\partial}{\partial x} (b + h) \approx \tau_b$
 - ice thickness and **volume** determined purely by **margin position** and **basal friction**
cf. Nye 1951, Weertman 1961, Ultee & Bassis 2016

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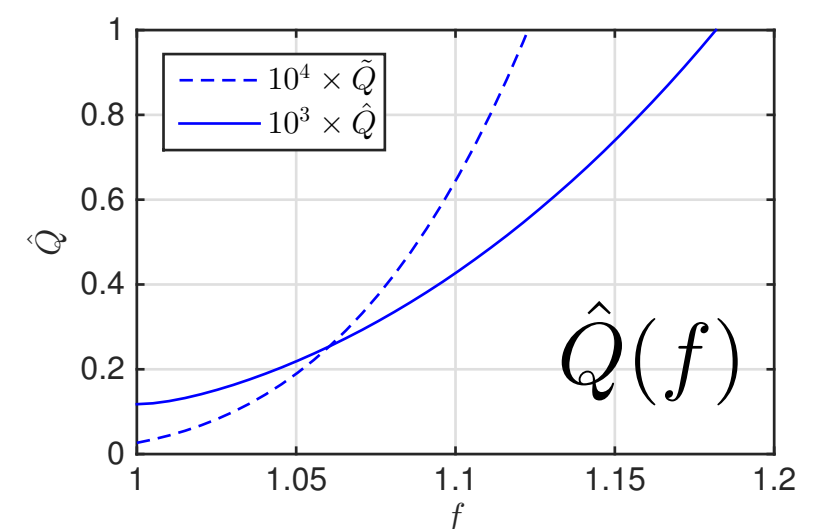
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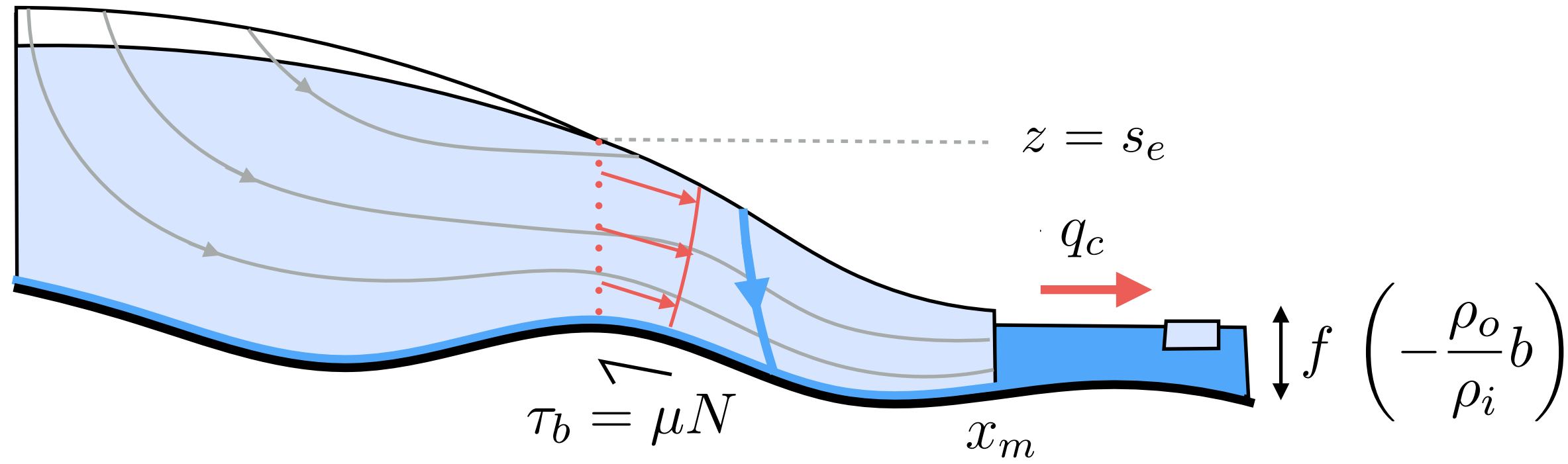
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- Near the front, a boundary-layer analysis relates **calving flux** to local **water depth**
cf. Schoof 2007, Tsai et al 2015

→ $q_c = \frac{A(2\rho_i g)^n}{\mu} \hat{Q}(f) \left(-\frac{\rho_i}{\rho_o} b \right)^{n+2}$

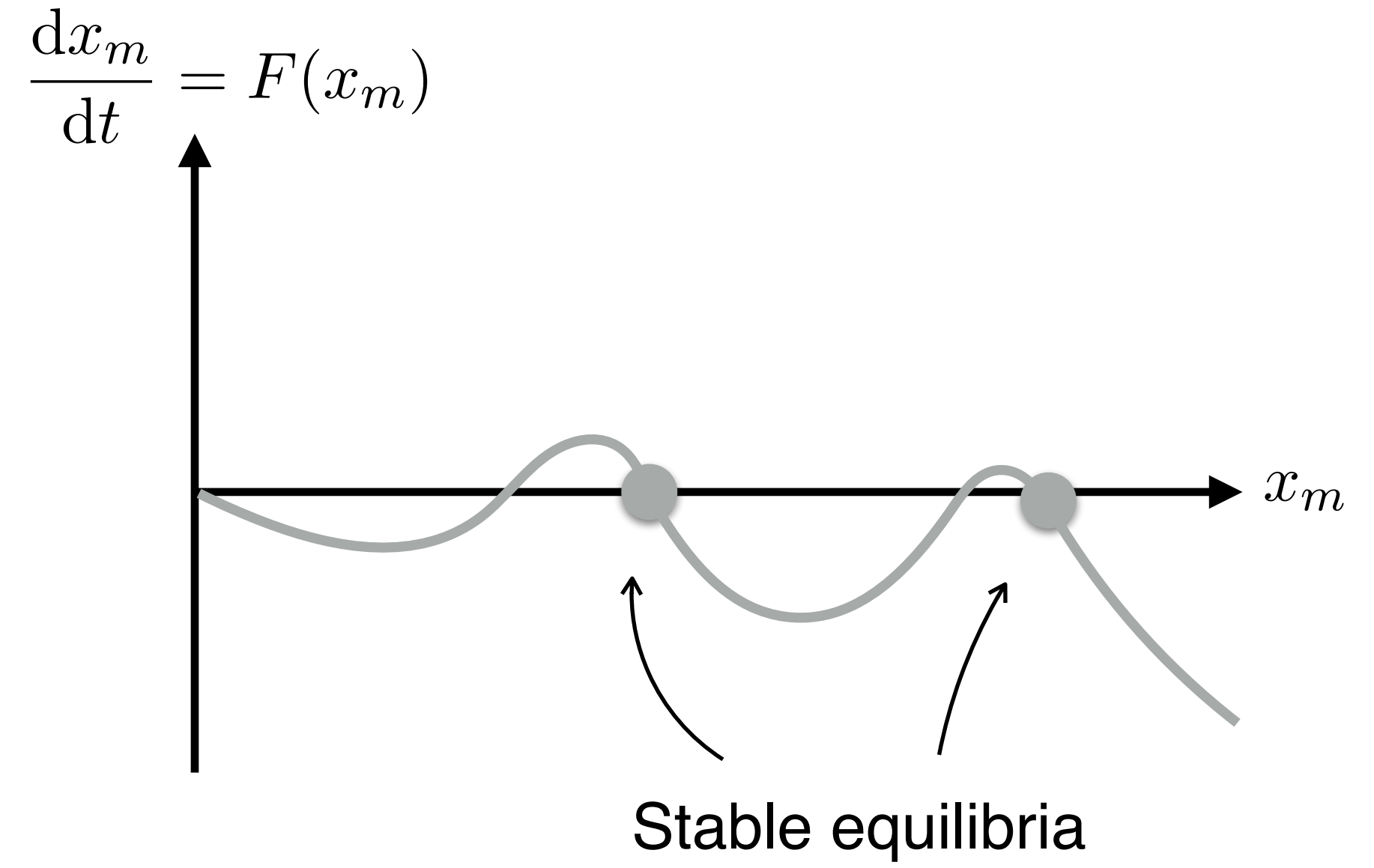


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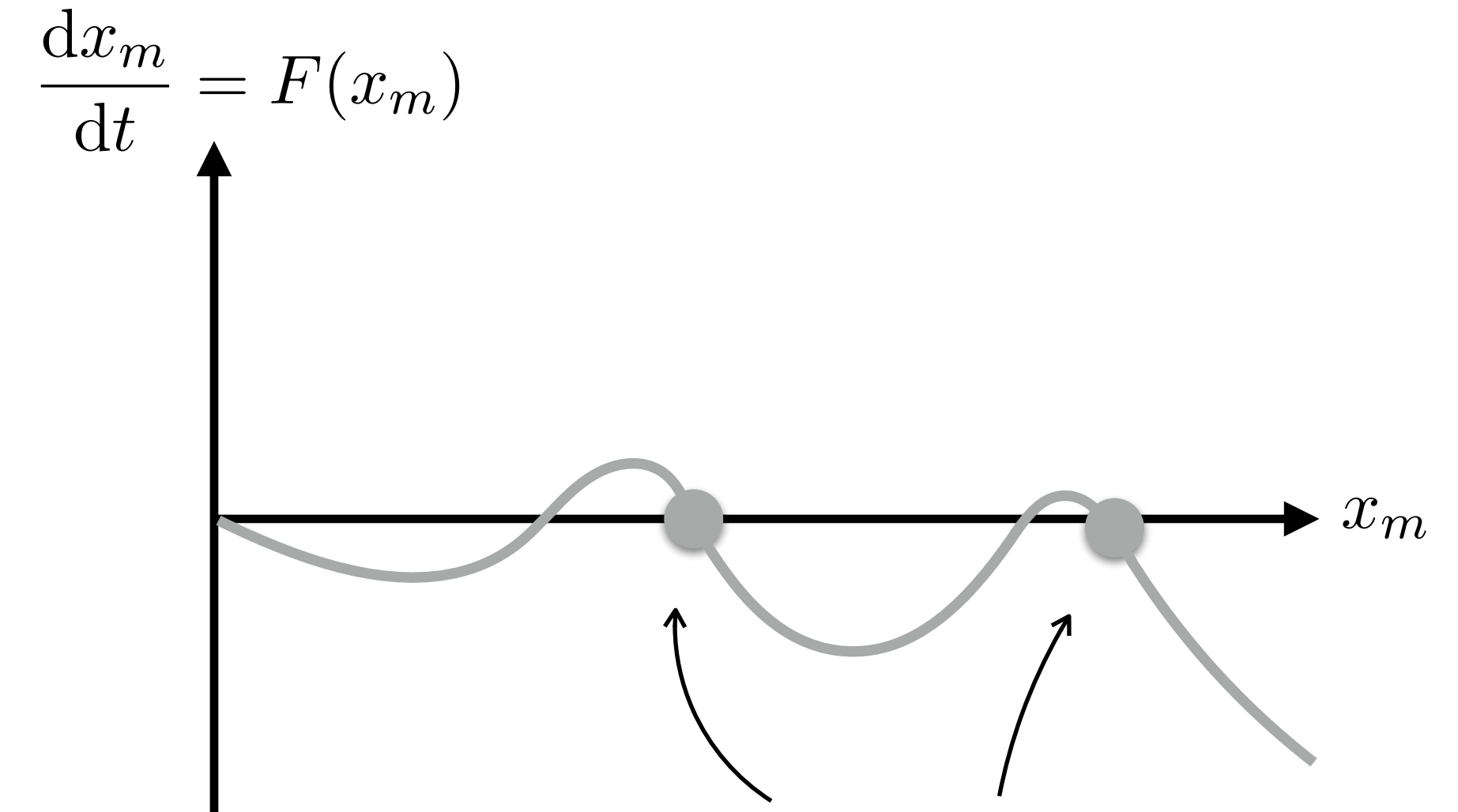
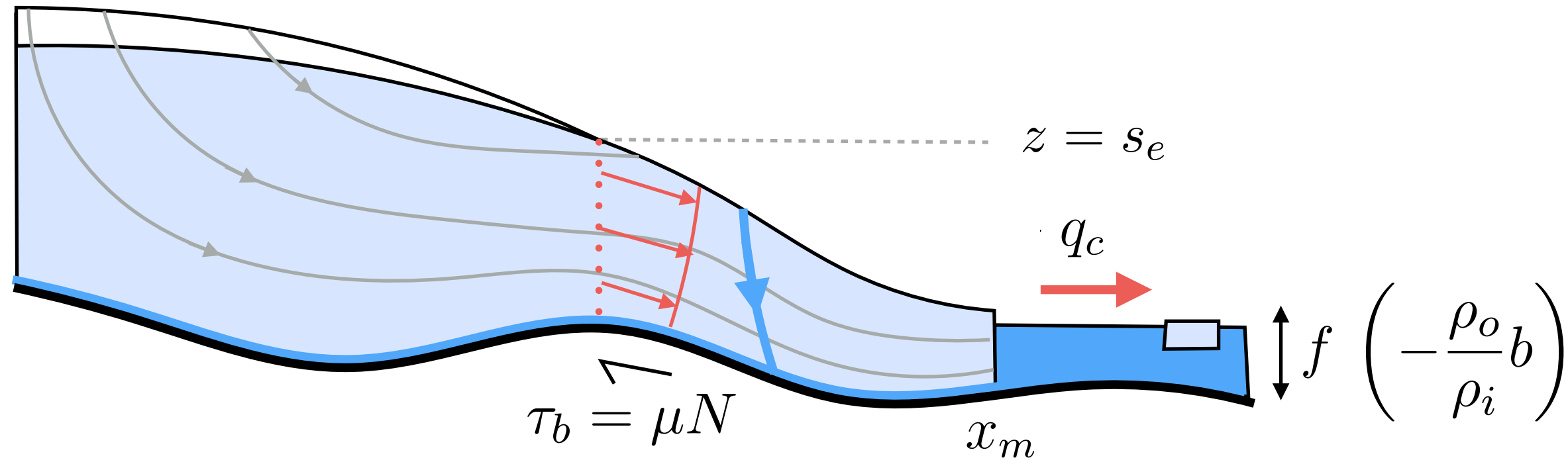


Global mass balance

$$\frac{dV}{dt} = q_b - q_c \quad \rightarrow \quad \boxed{\frac{dx_m}{dt} = F(x_m; N, s_e, f)}$$



A simplified model of a tidewater glacier



Global mass balance

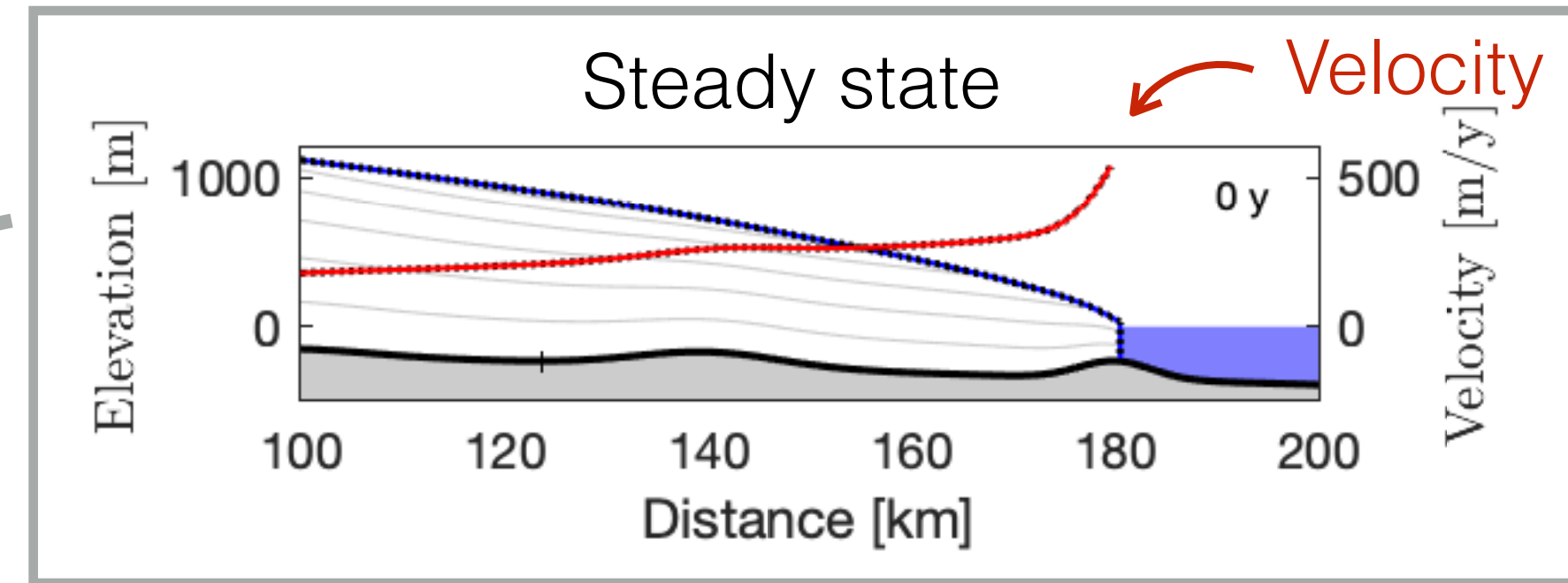
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Forcing parameters:

- N Bed strength
- s_e Equilibrium line altitude (ELA)
- f Calving parameter

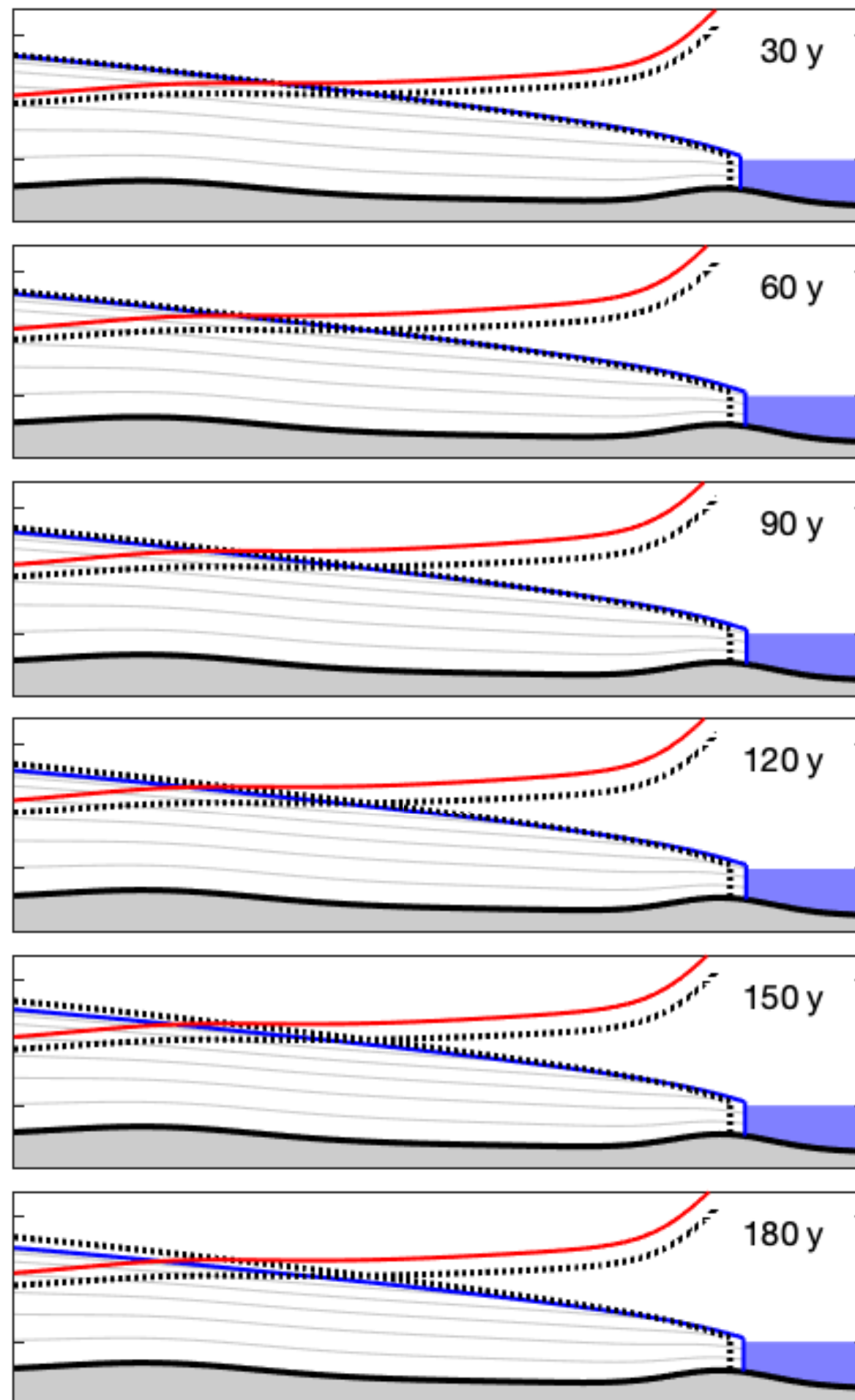
Motivation: impact of subglacial lubrication



Decreasing basal friction

Increasing basal friction

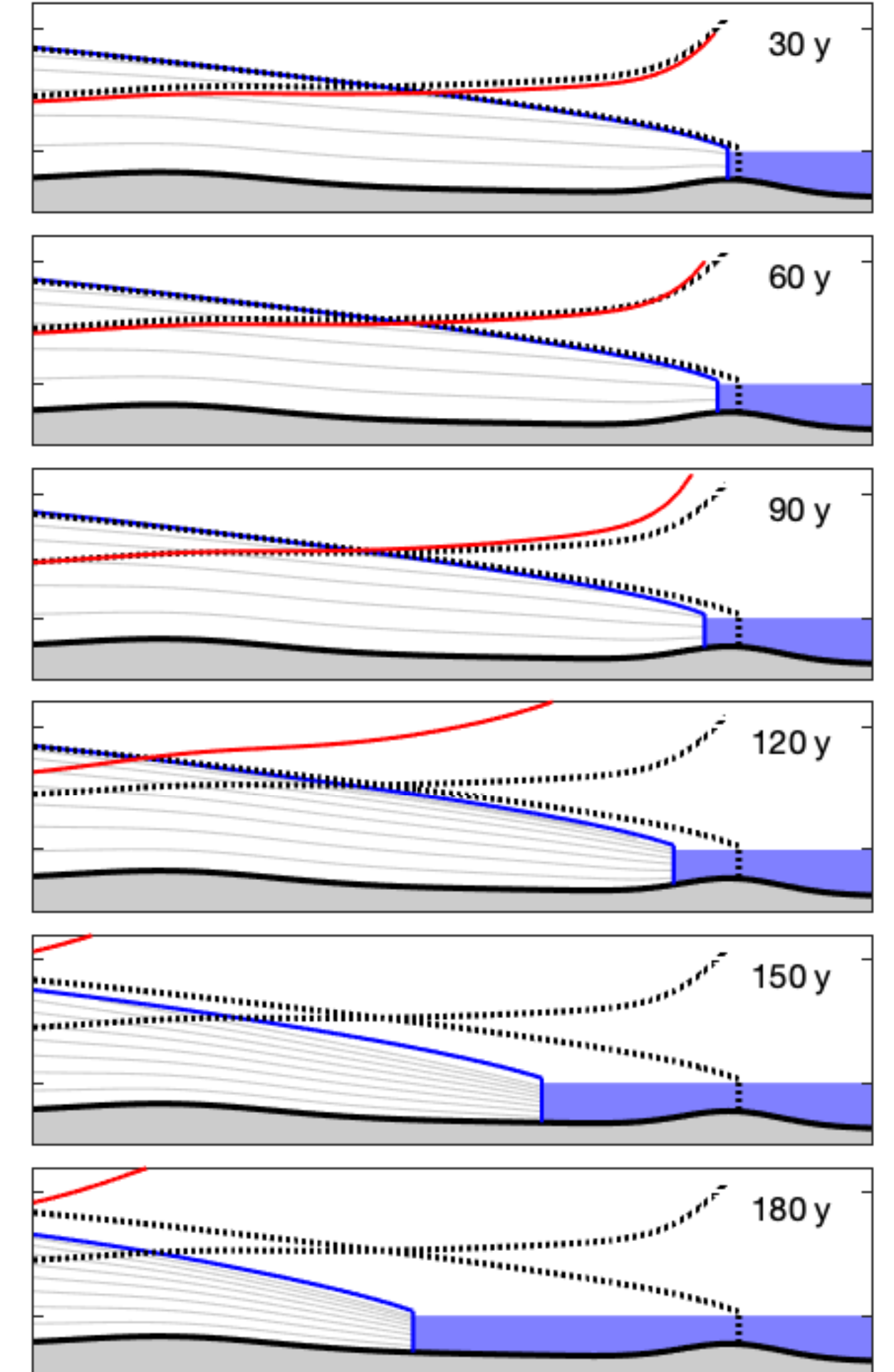
Time ↓



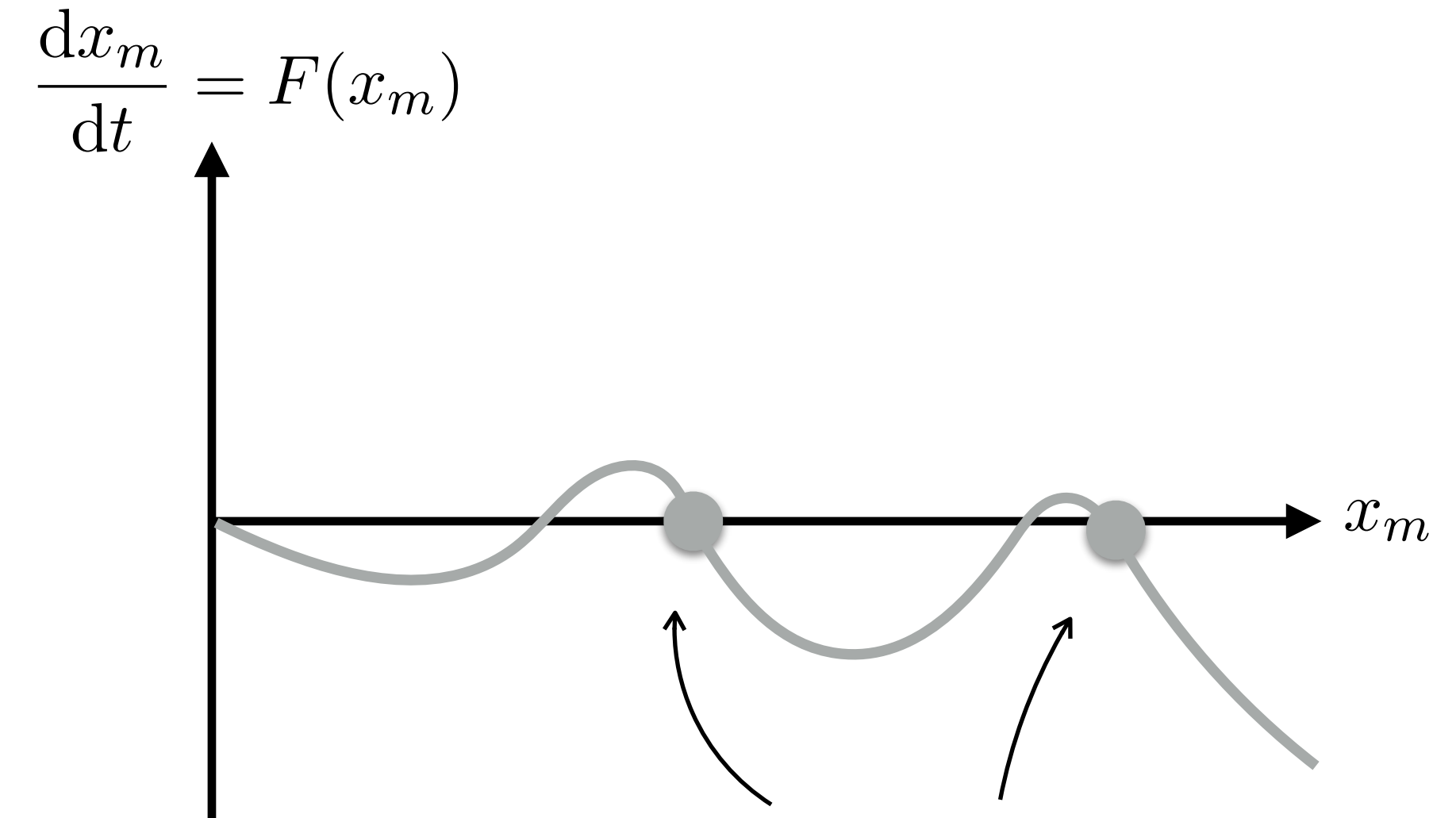
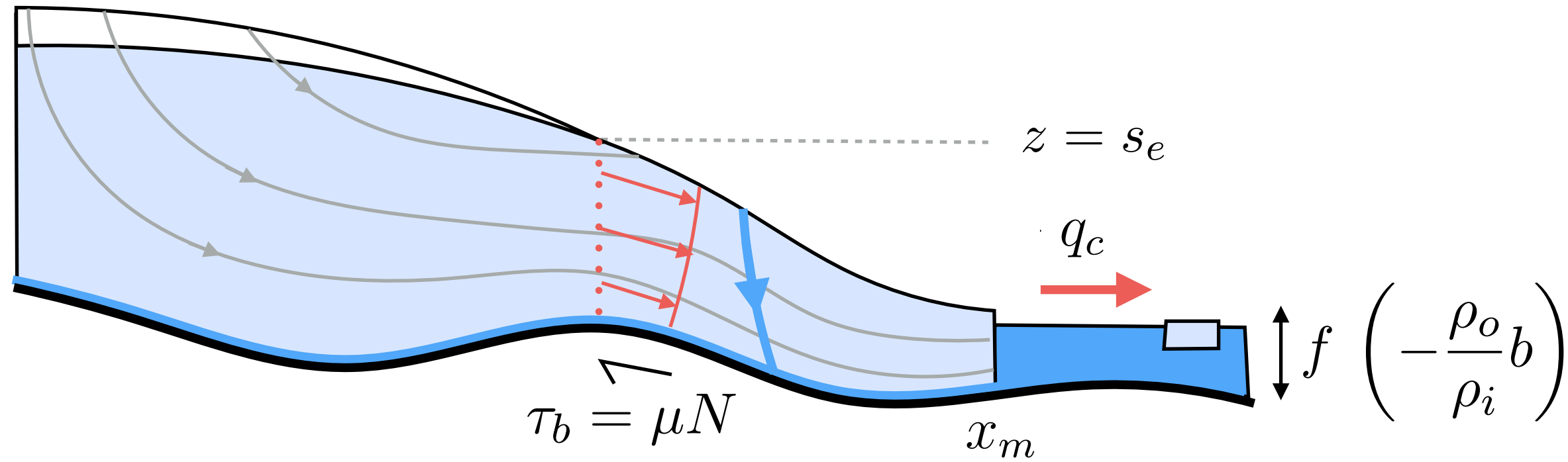
Speed up
↓
Advance
↓
Increased mass loss

Slow down
↓
Retreat
↓
Speed up

Greater mass loss



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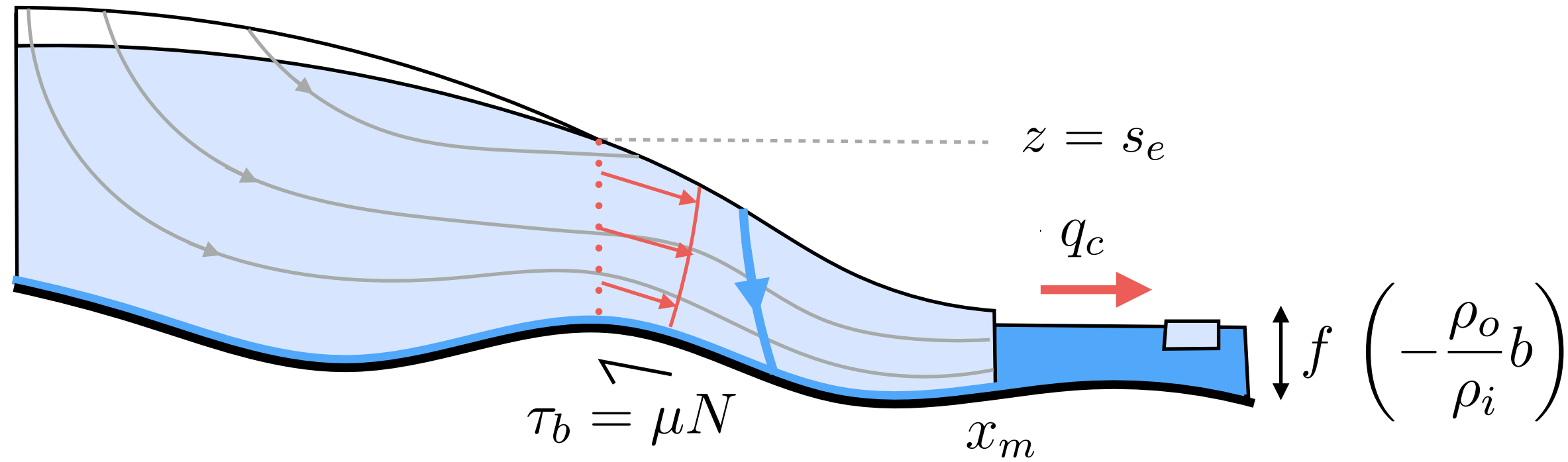
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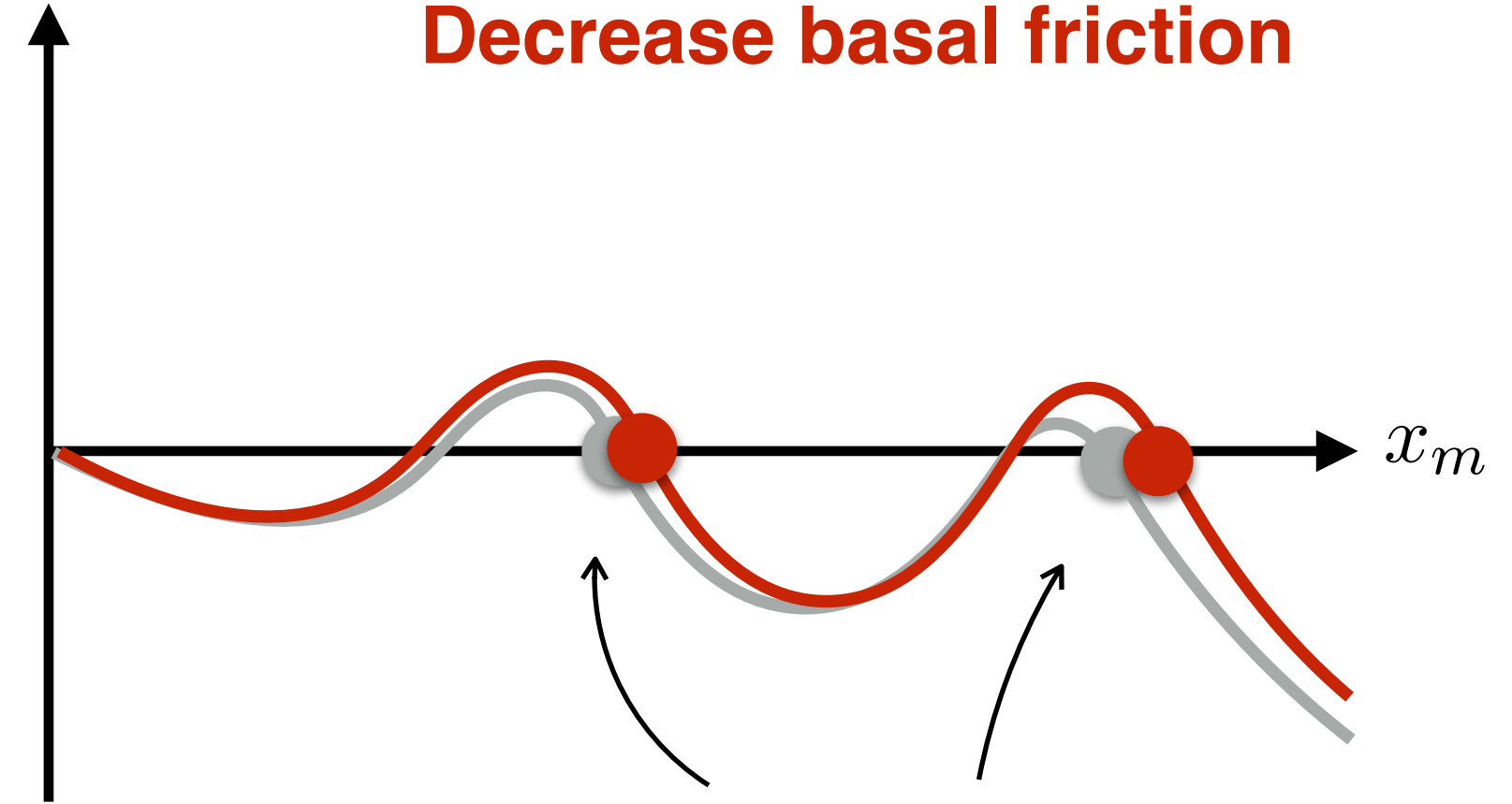
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Decrease basal friction



Stable equilibria

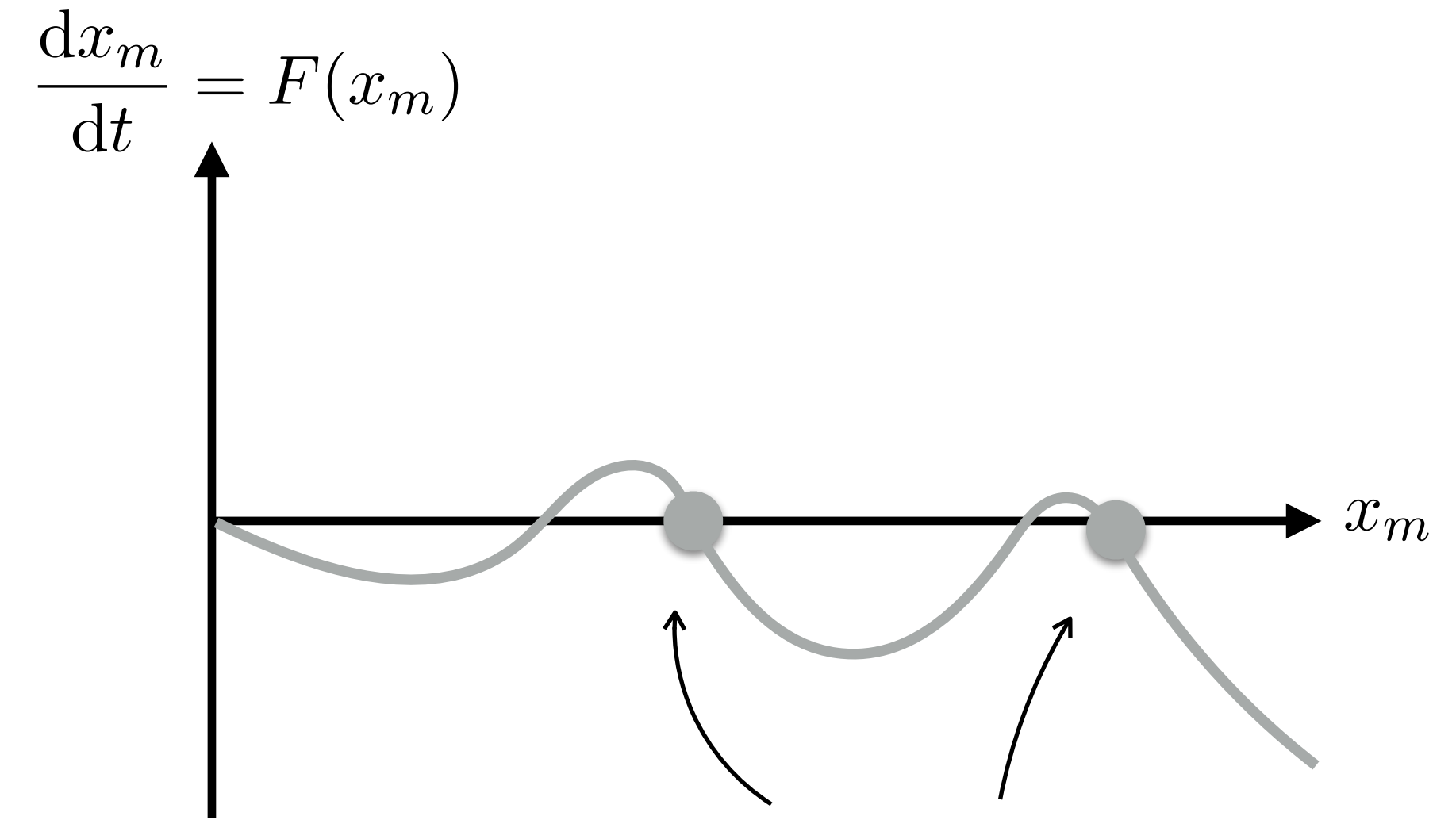
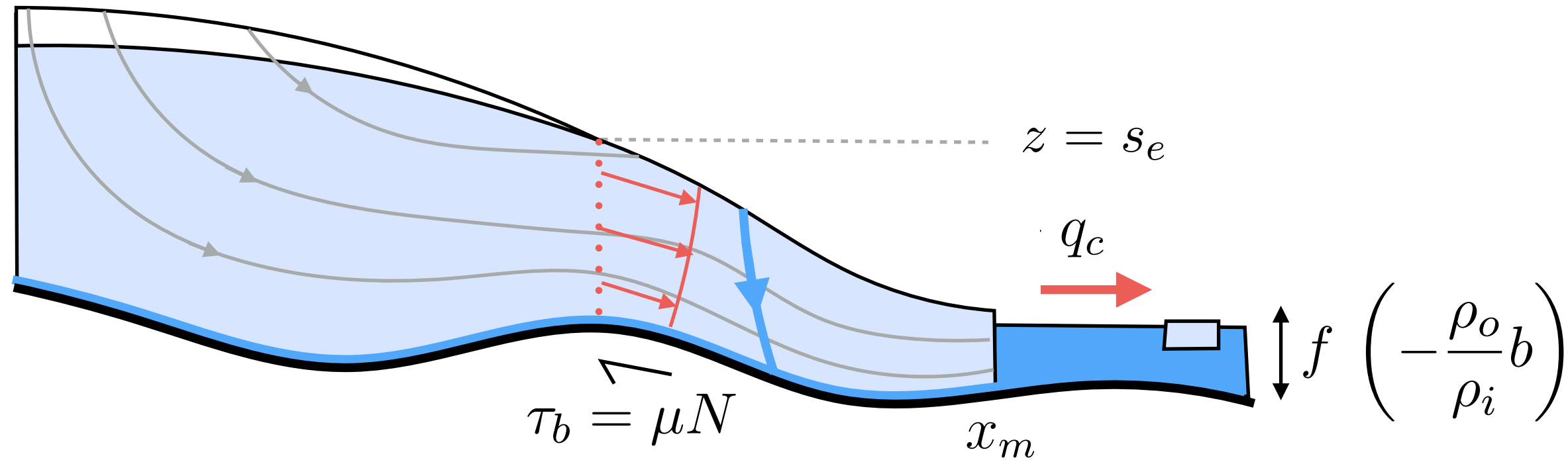
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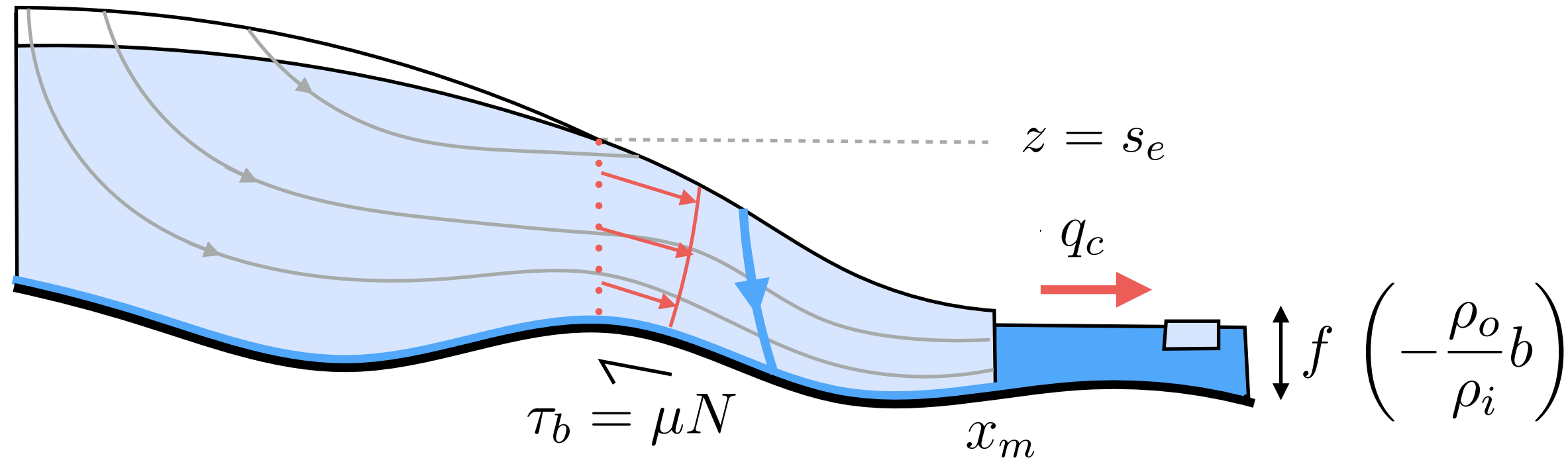
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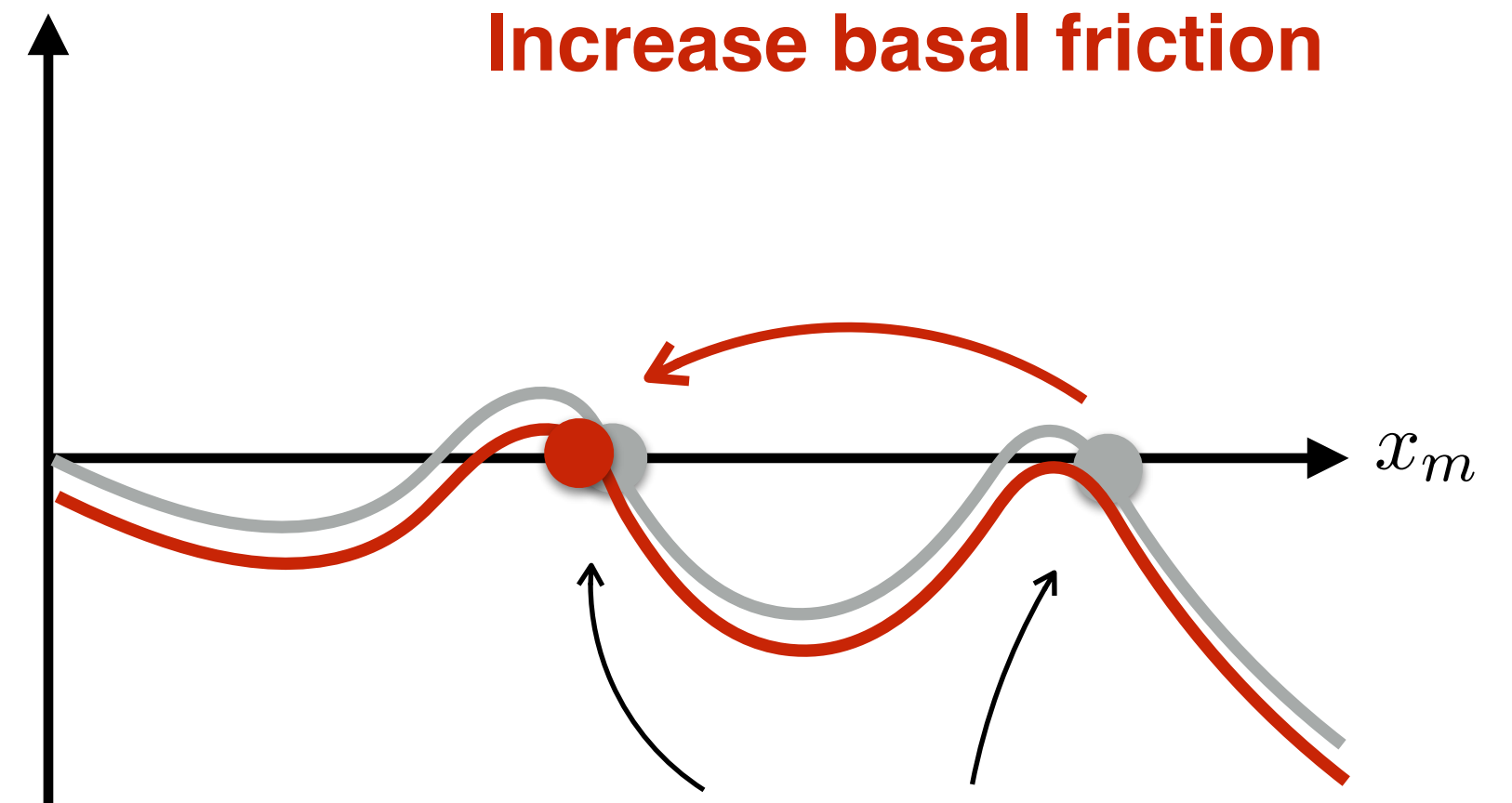
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Increase basal friction



Stable equilibria

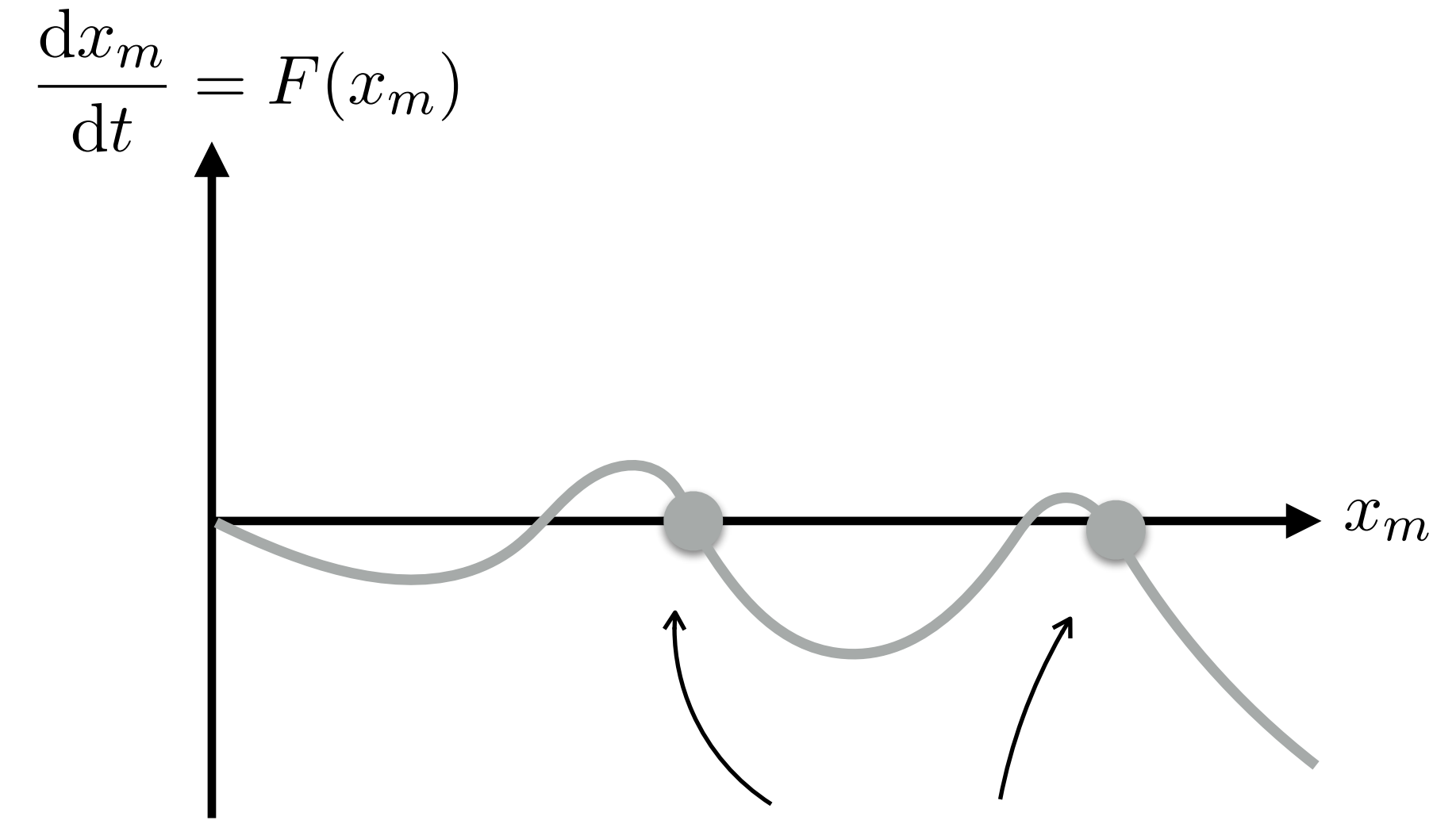
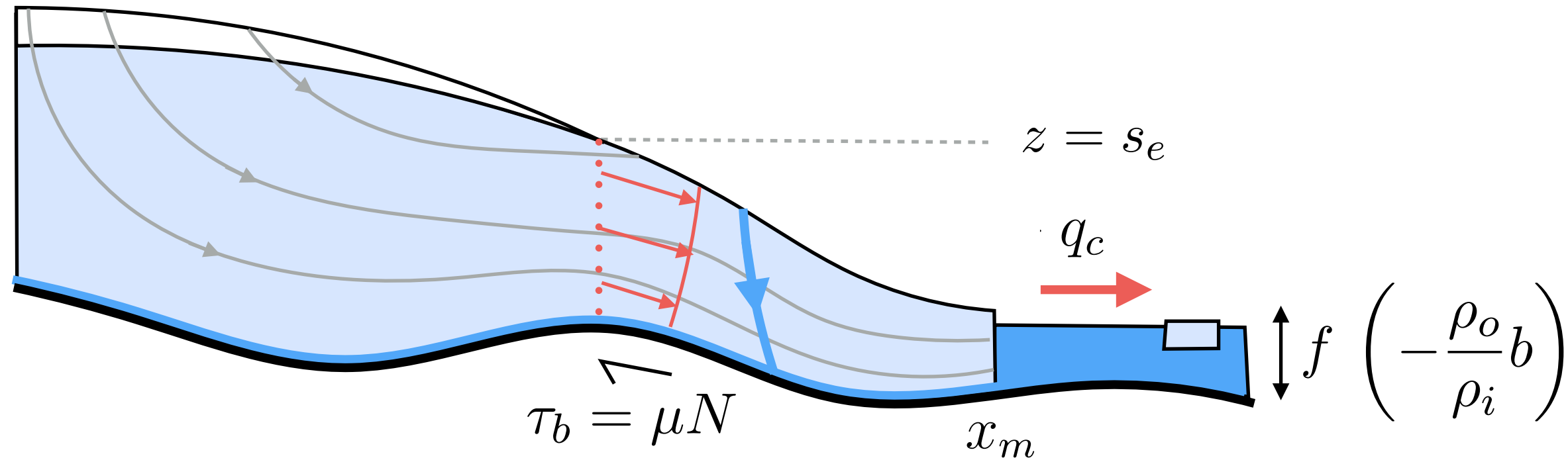
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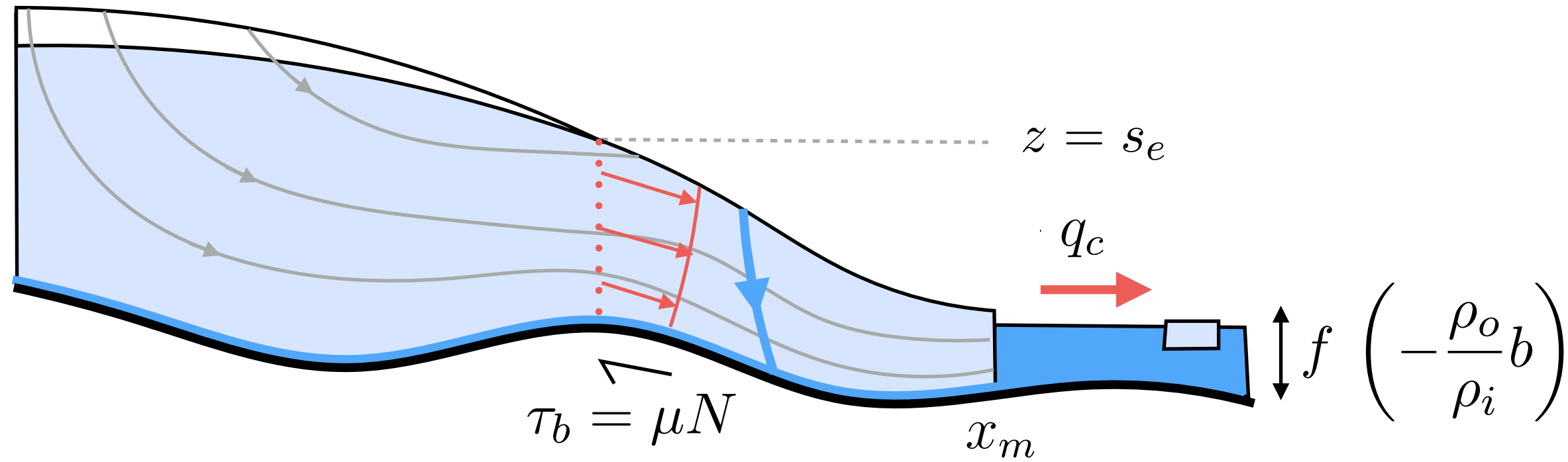
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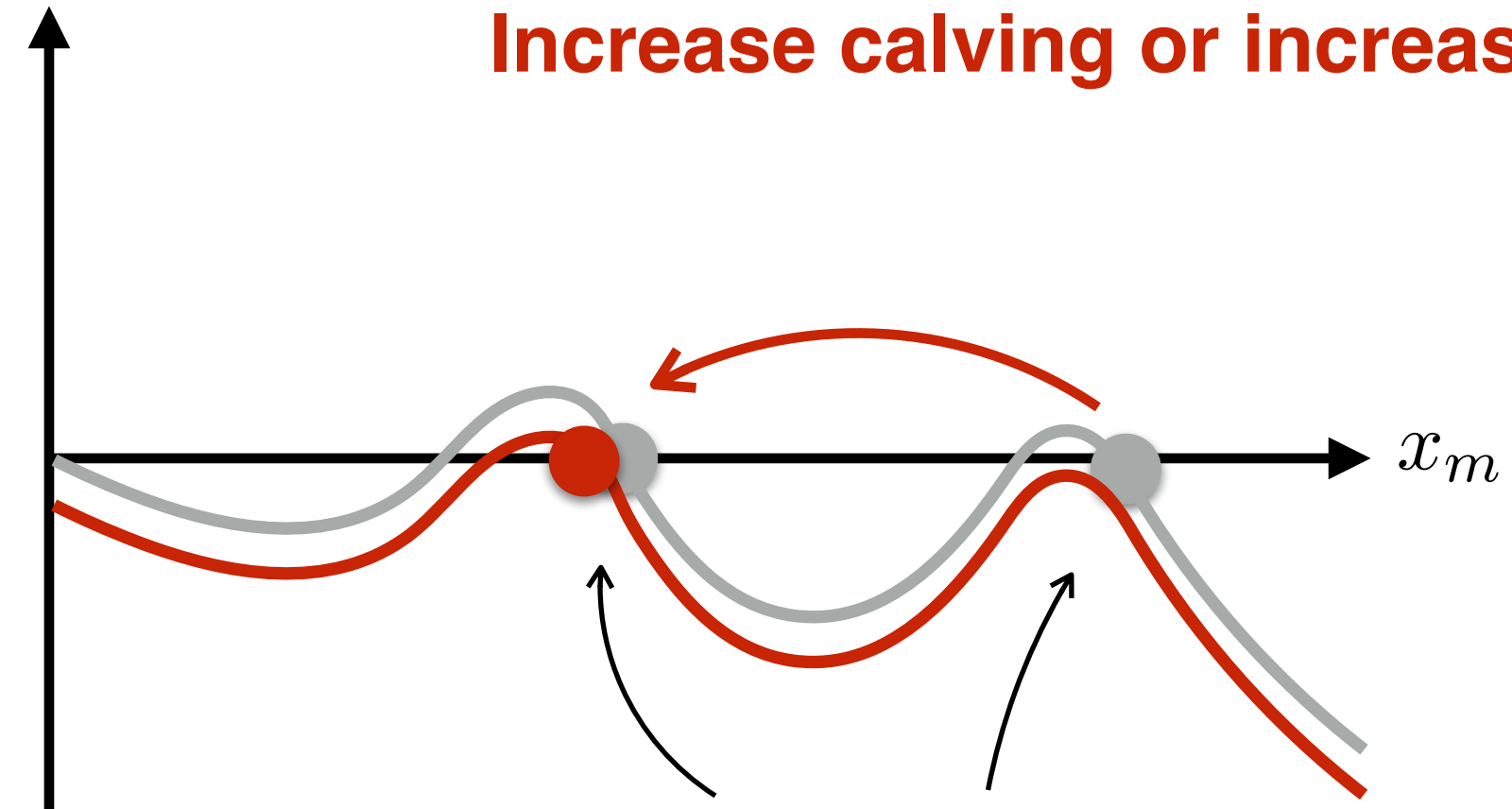
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Increase calving or increase ELA



Stable equilibria

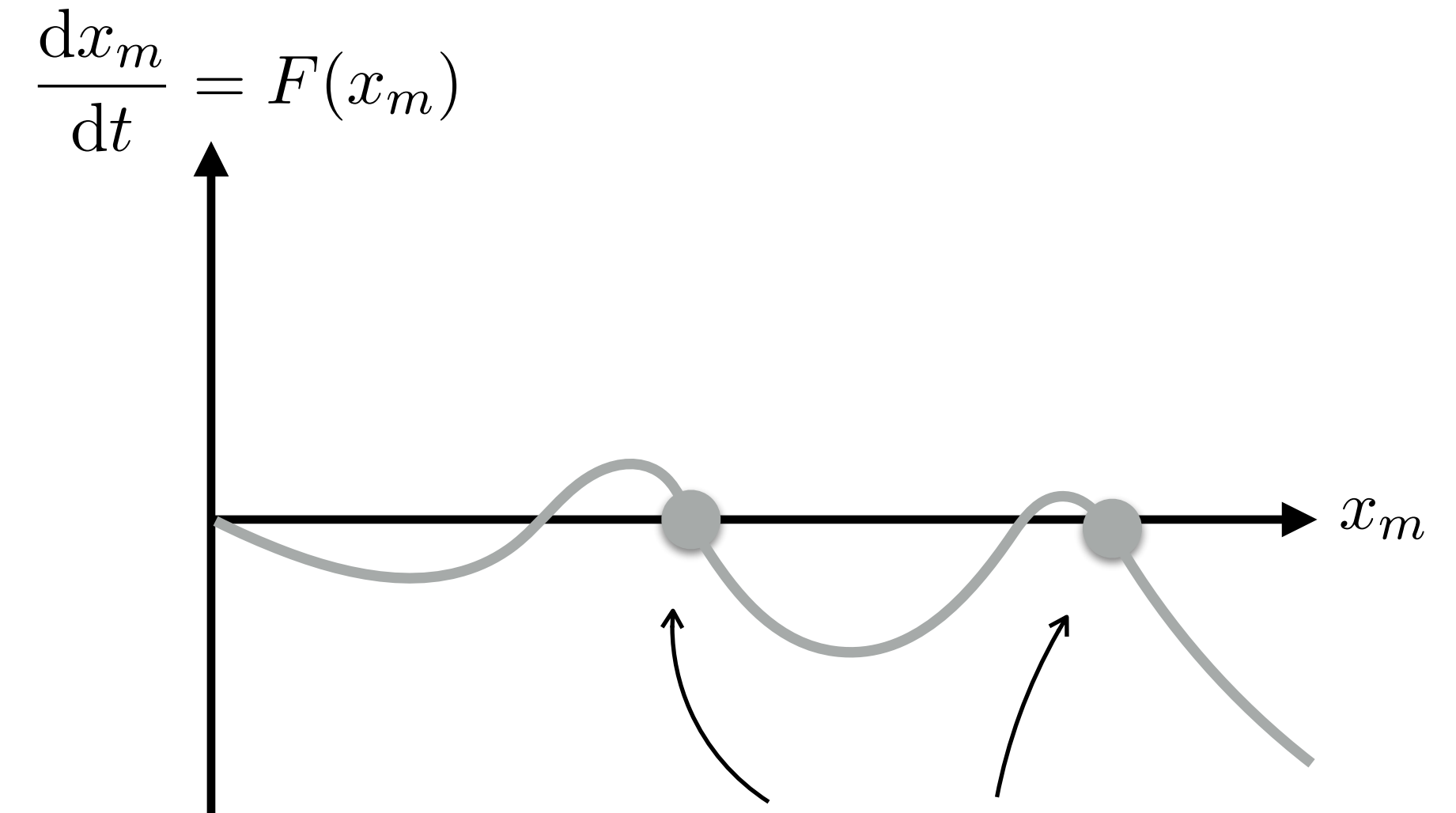
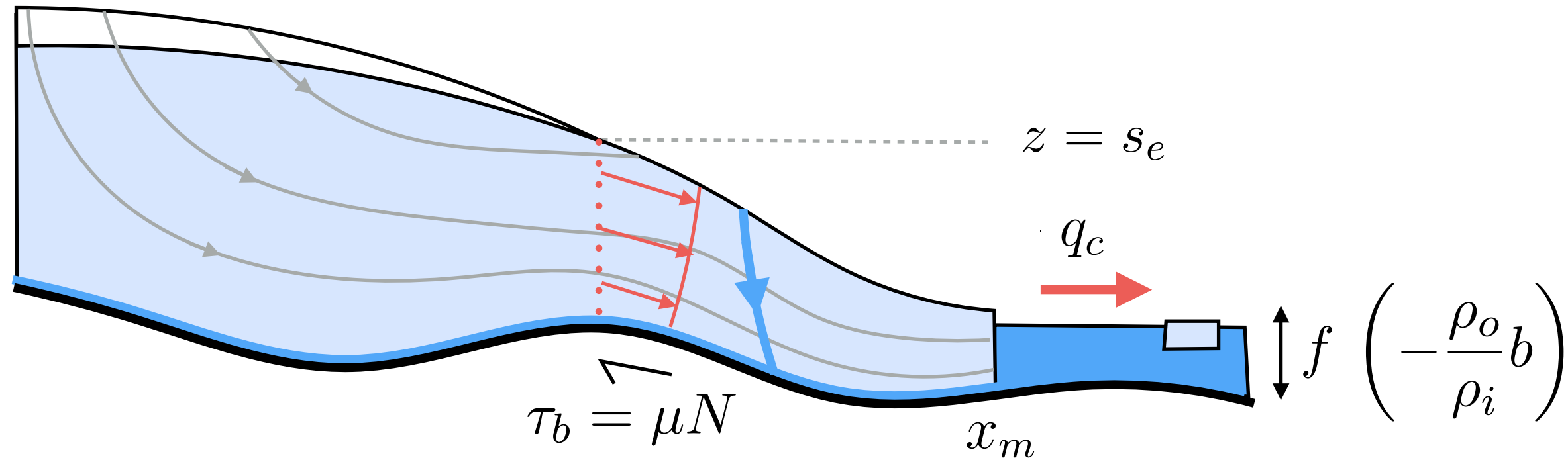
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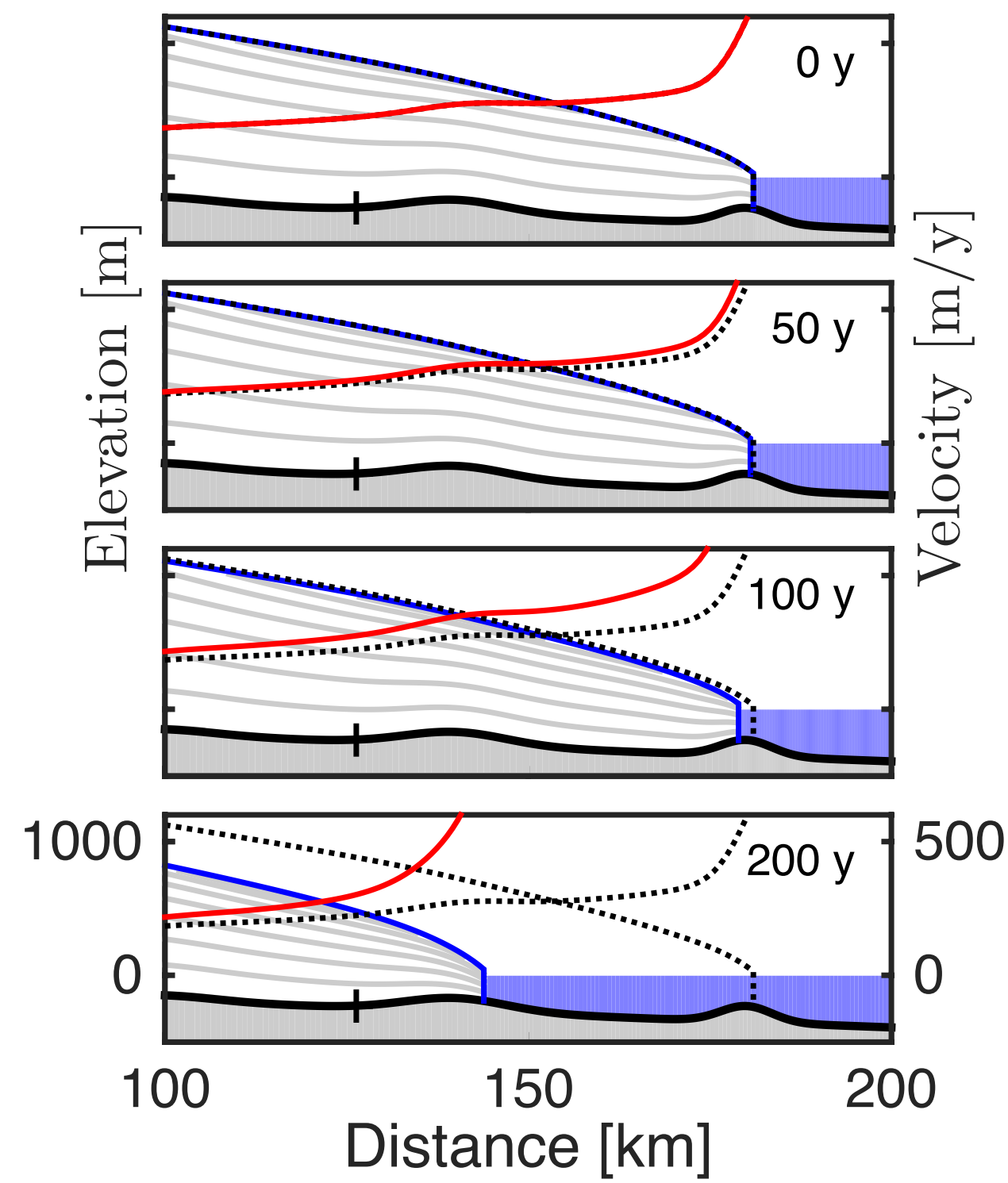
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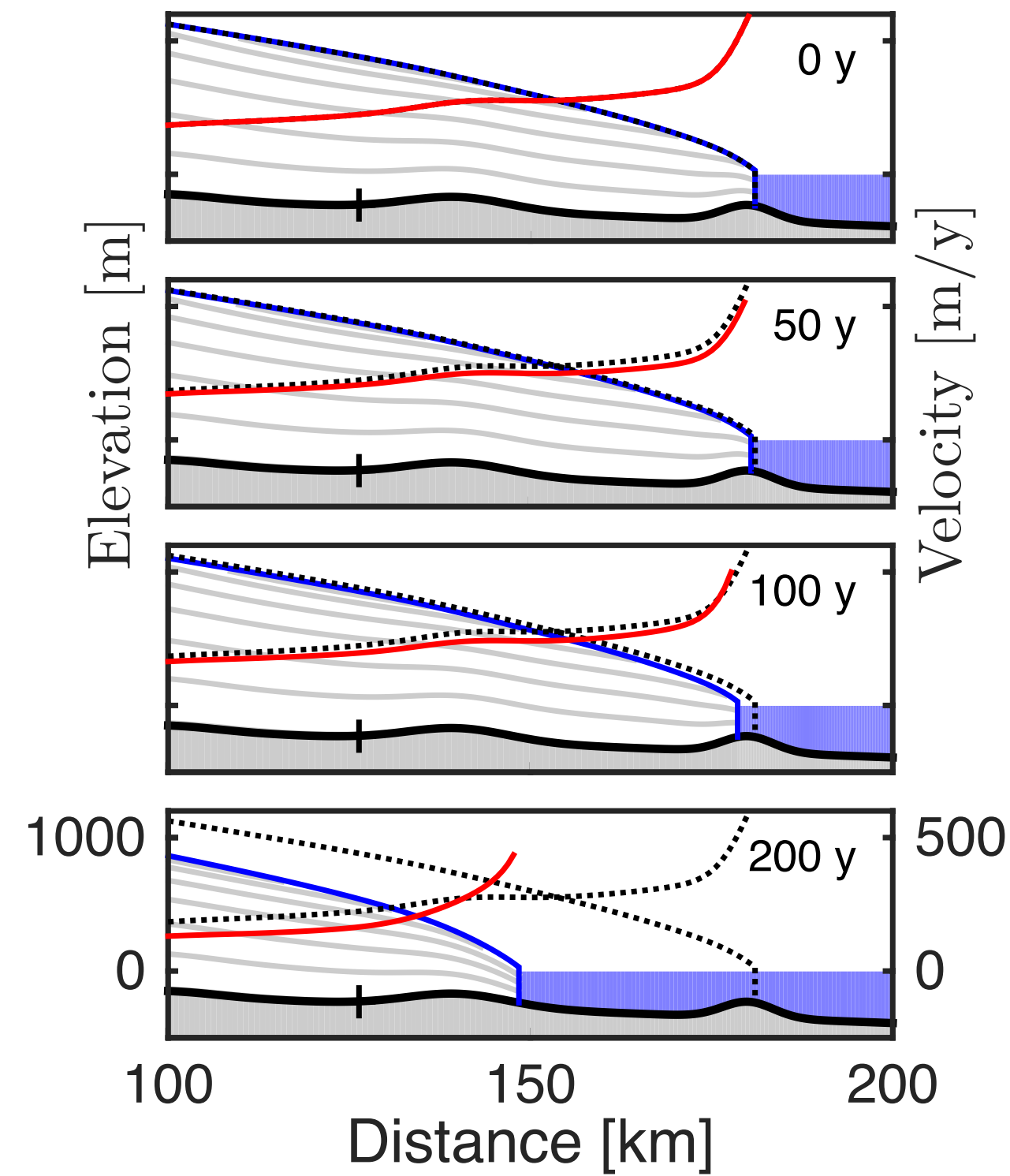
Response to different forcing

An essentially **indistinguishable** response can occur to very distinct forcing mechanisms.

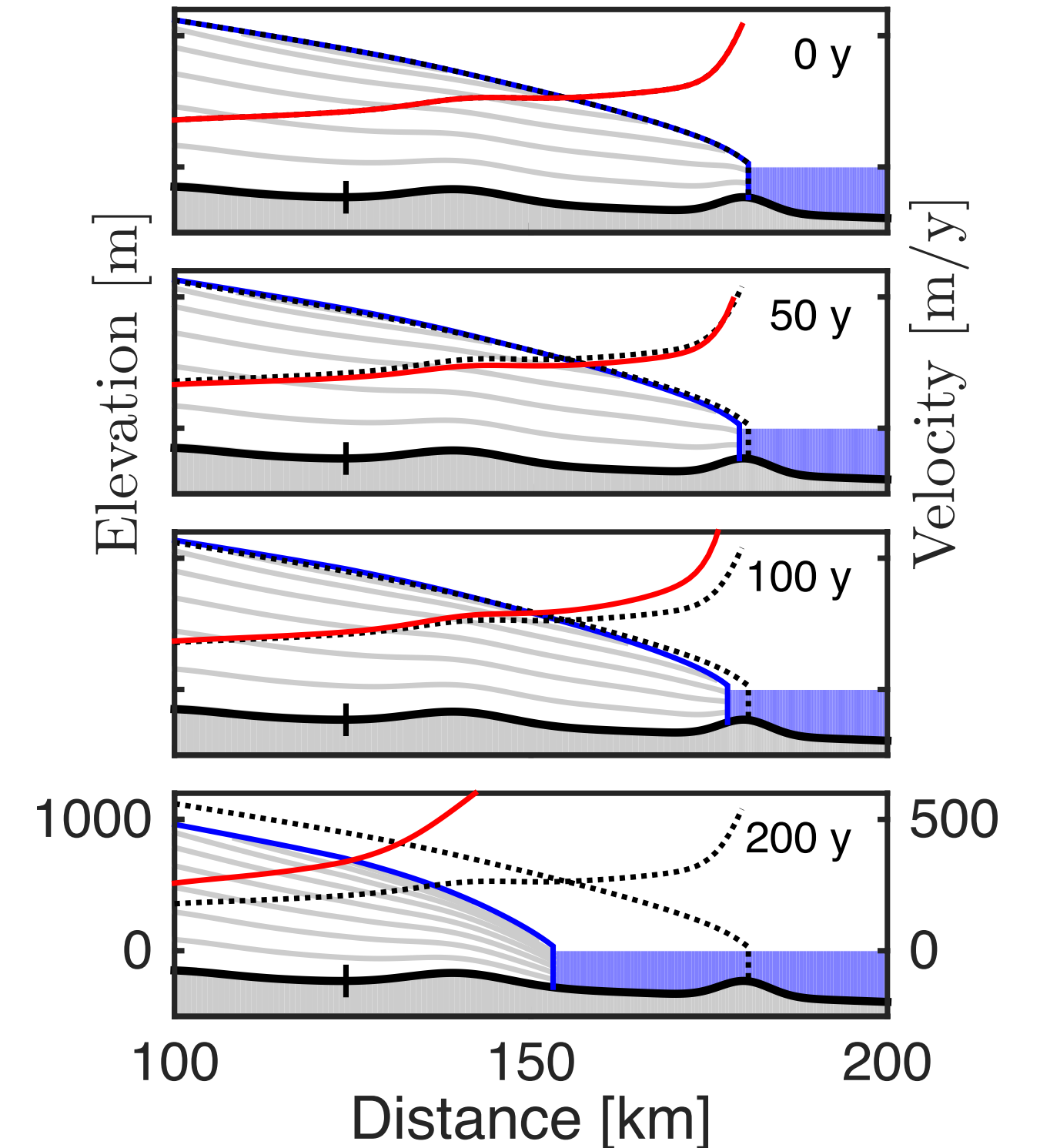
Increased calving



Increased ELA

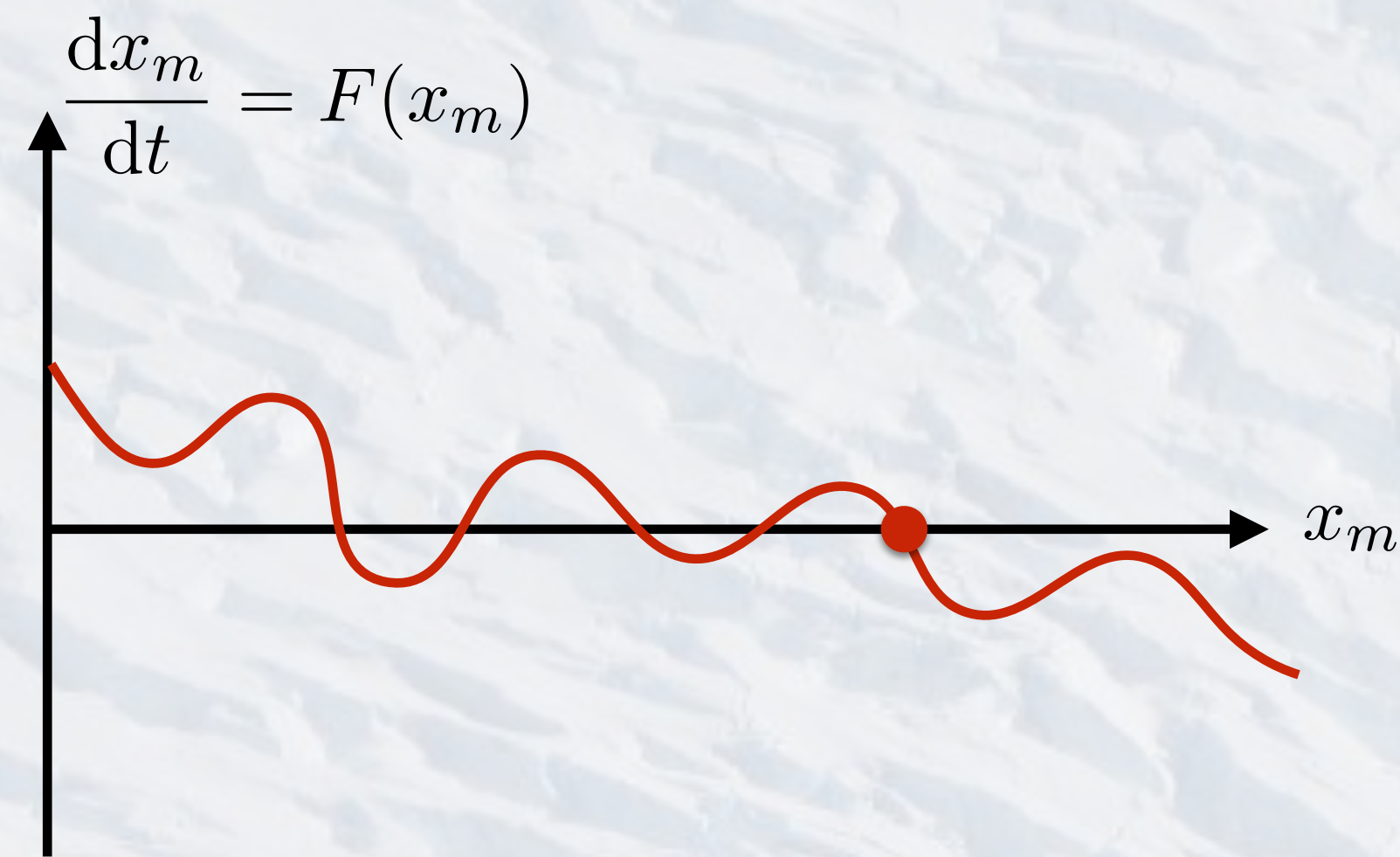


Increased bed strength



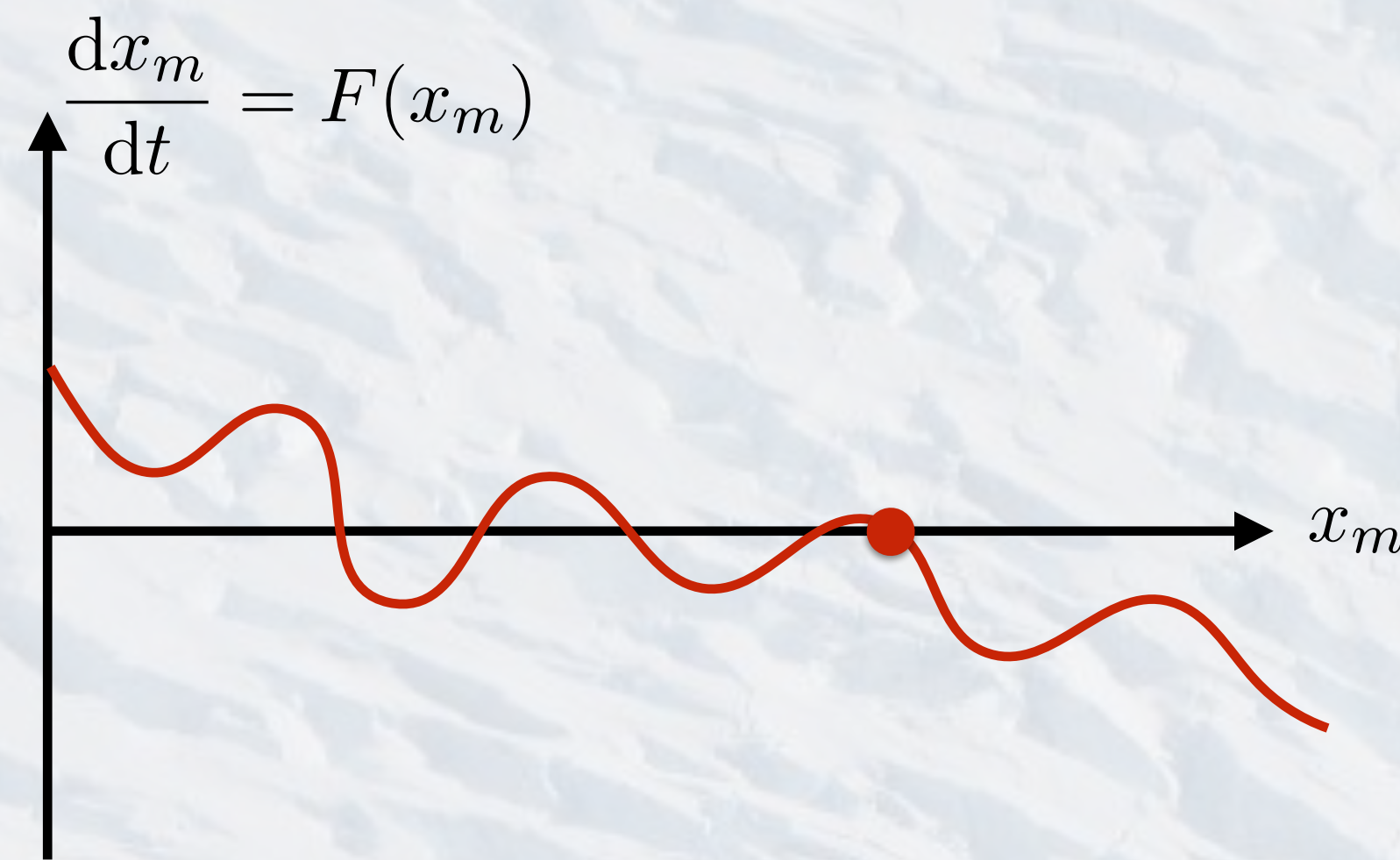
Summary

- Tidewater glaciers can be described as **a forced dynamical system**.
- **Episodic acceleration and deceleration** of a tidewater glacier is **generic**, in response to changes in **both oceanic and upstream** forcing.



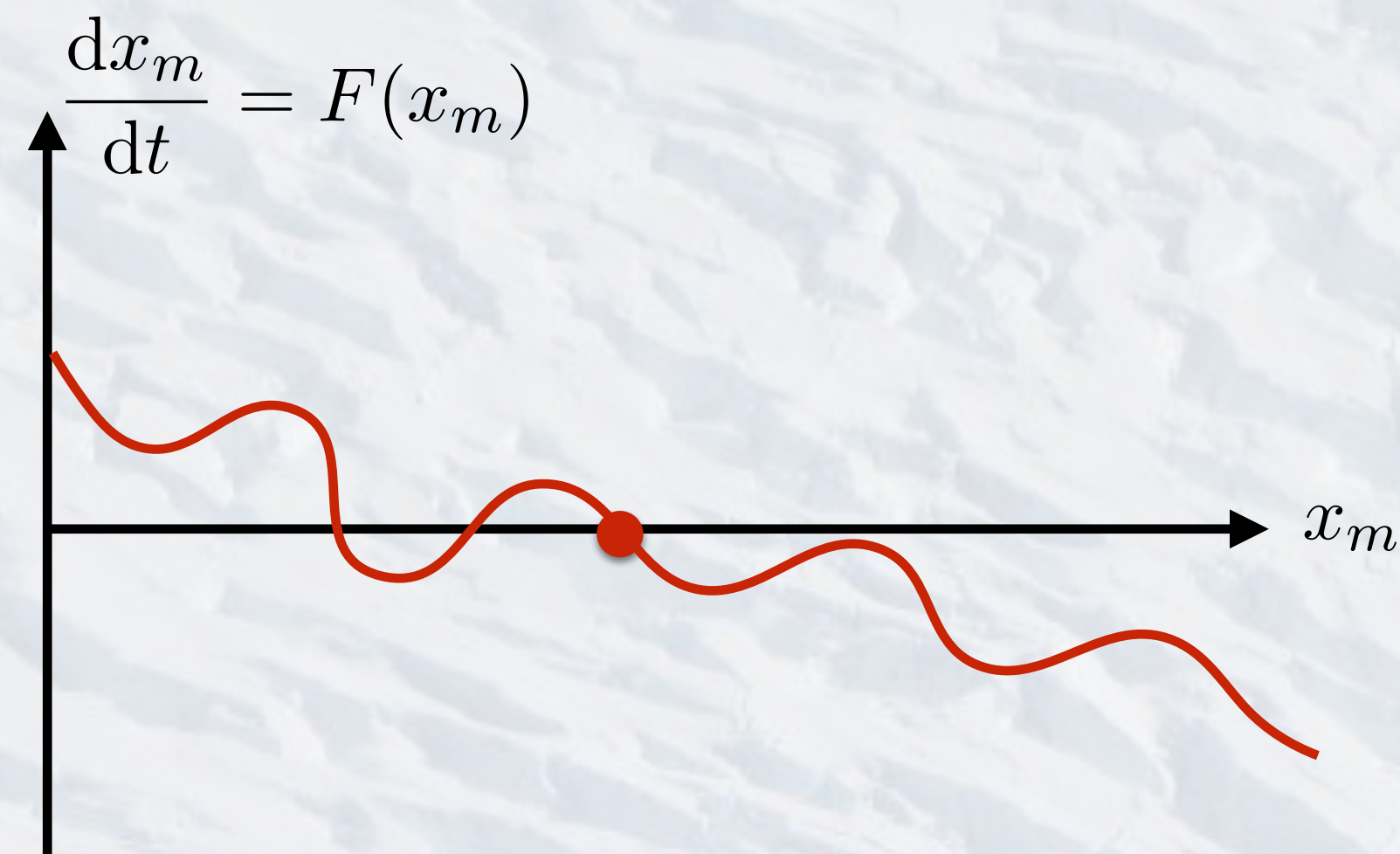
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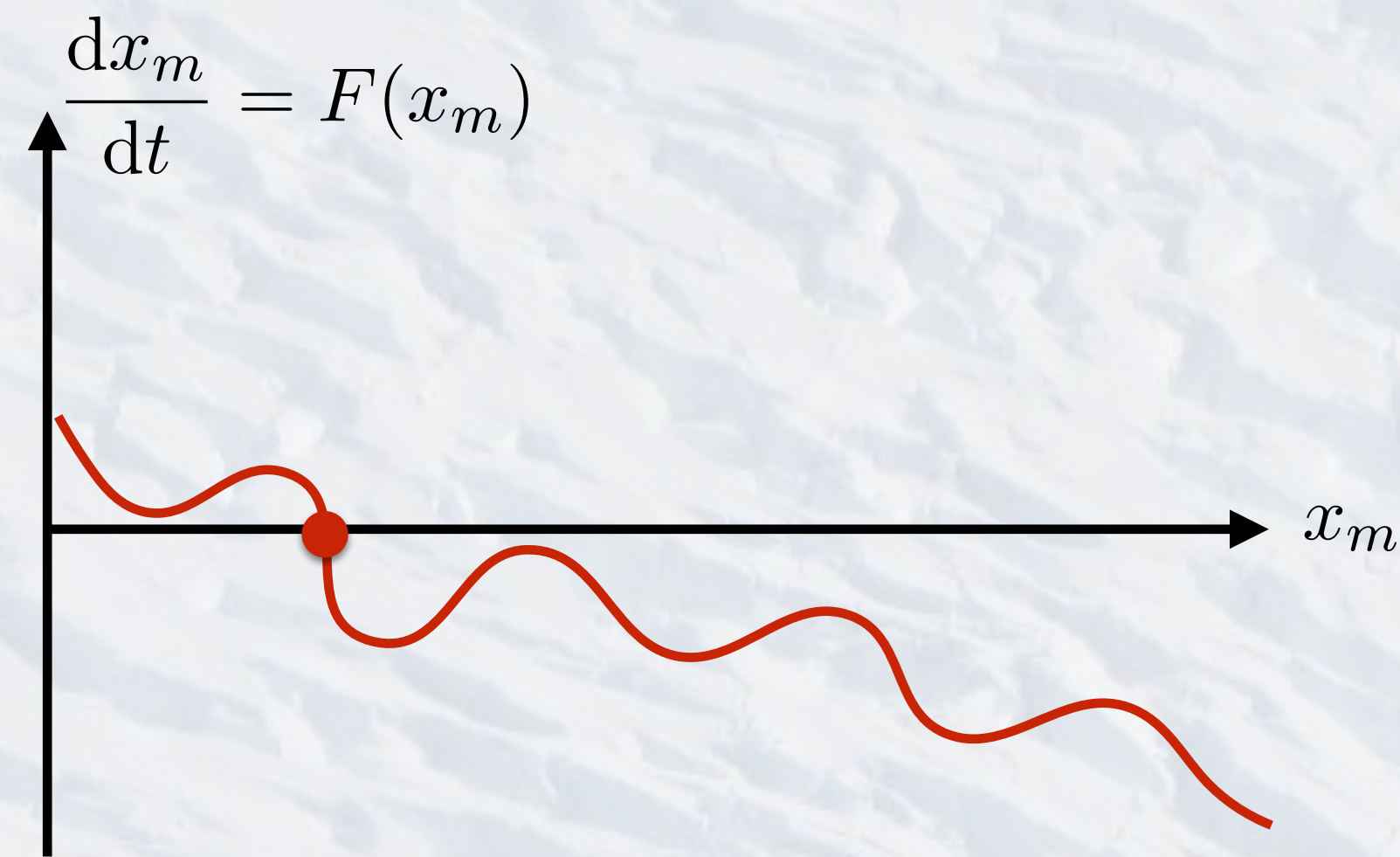
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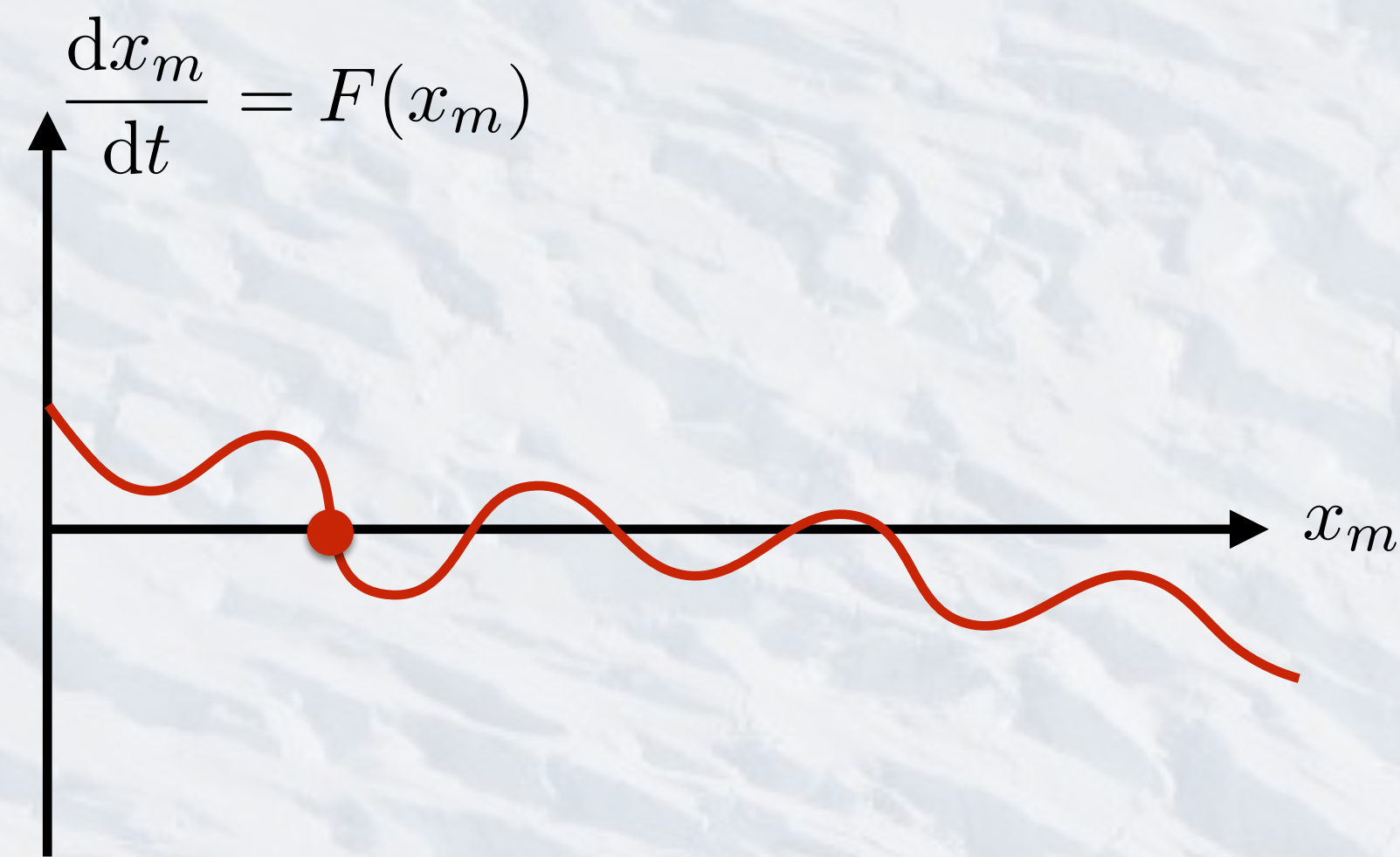
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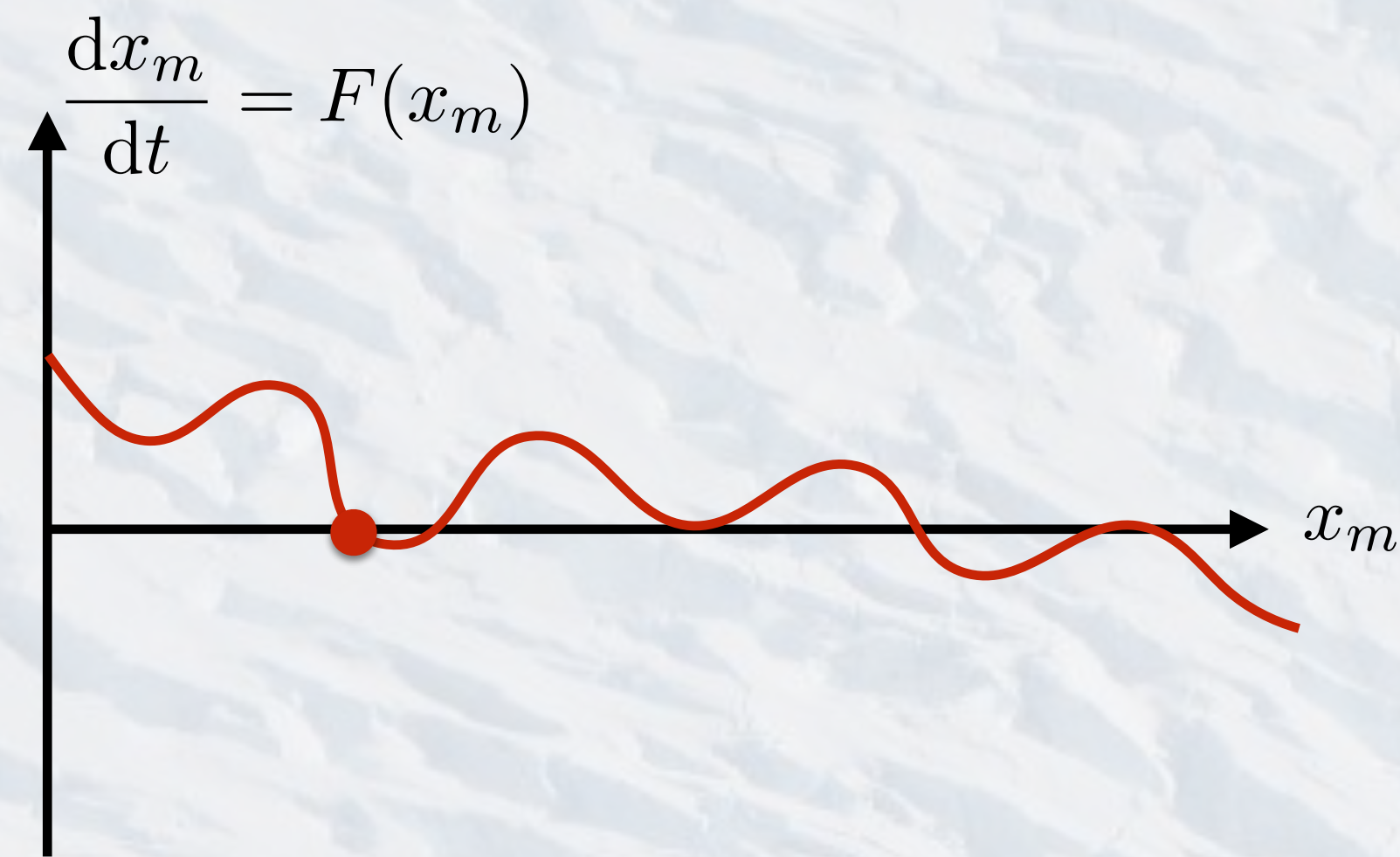
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