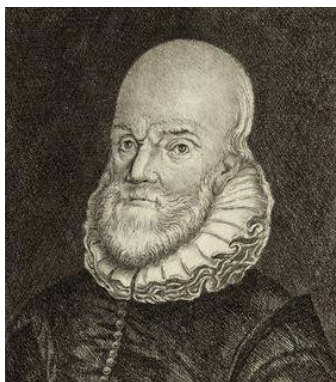




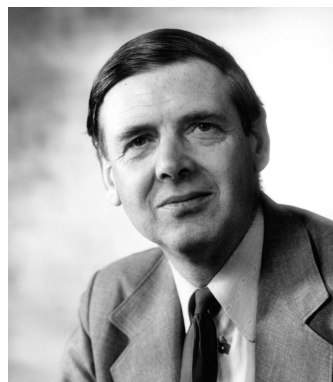
# Mathematics of Ice

Ian Hewitt

# Trinity Maths Fellows



Thomas Allen (1564-1571)



John Hammersley (1961-1985)



Chris Prior (1976-2013)



Simon Salamon (1984-2001)



Bernd Kircheim (2002-2012)



**Ian Hewitt (2013-)**



Steve Shkoller (2013-2014)



**Melanie Rupflin (2015-)**

# Trinity Maths Today

2 fellows

21 undergraduates (BA / MMath)

7 graduate students (MSc / DPhil)



new Mathematical Institute (2013)





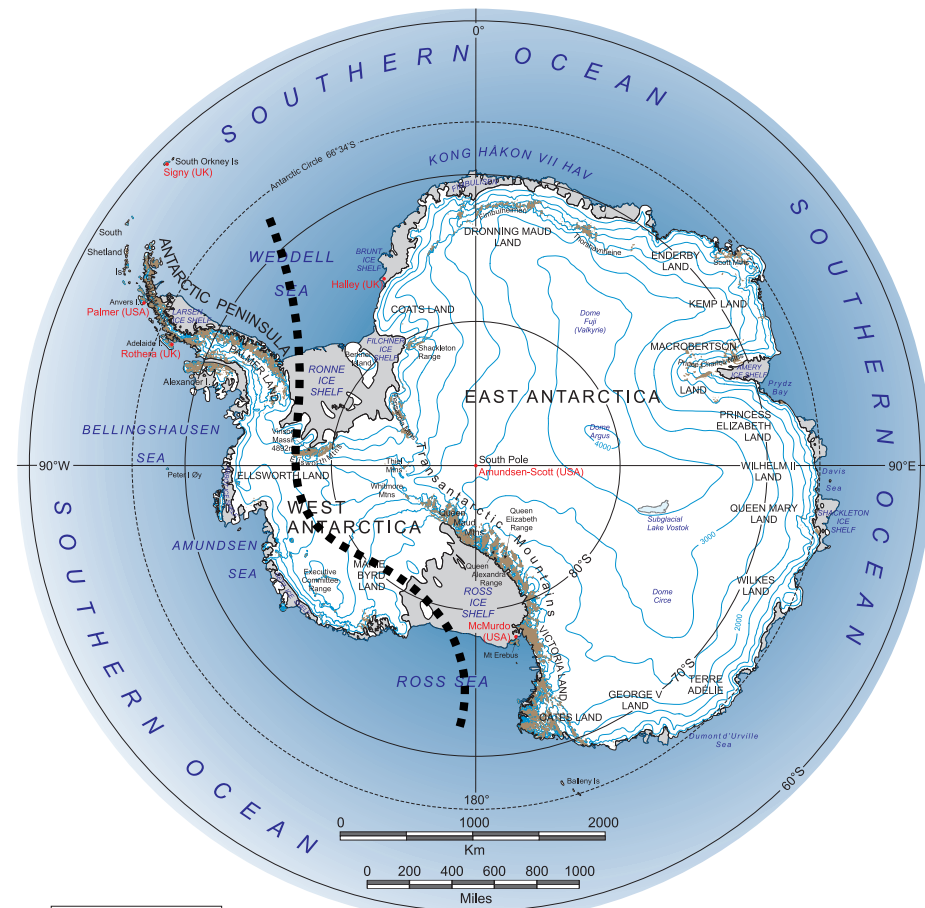




current sea level rise  
 $\approx 3.2 \text{ mm/y}$

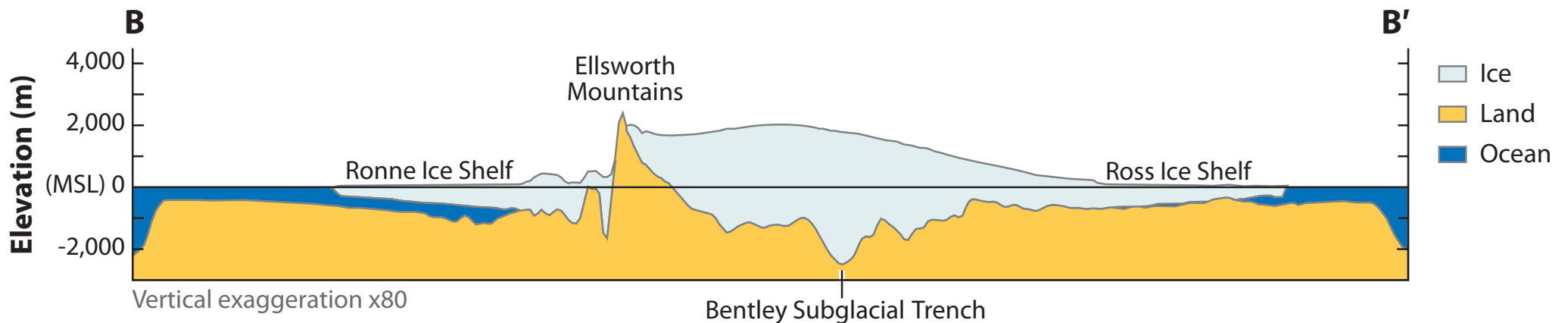
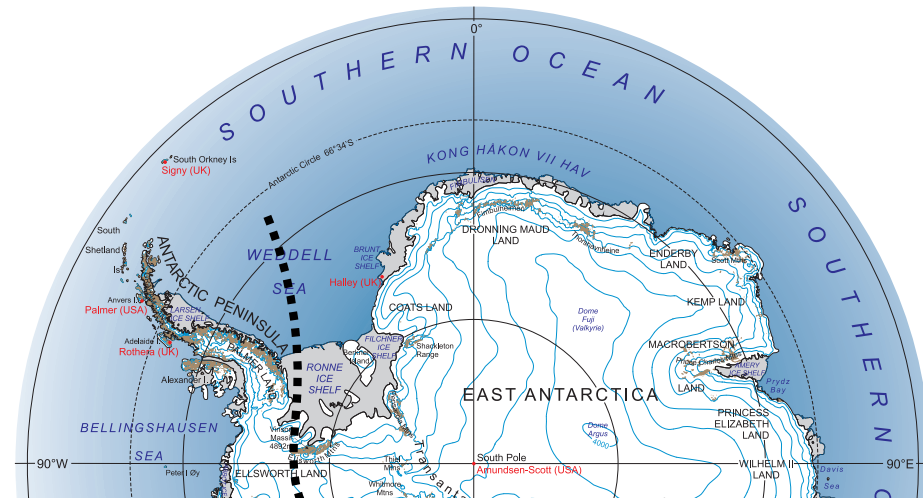
# Ice sheets

The Antarctic and Greenland ice sheets contain water equivalent to approximately 65 m sea level.



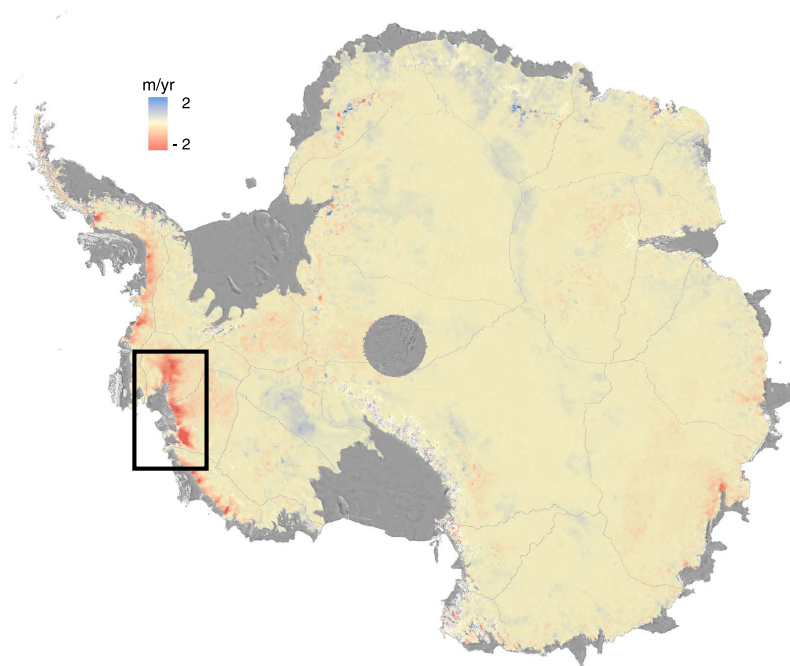
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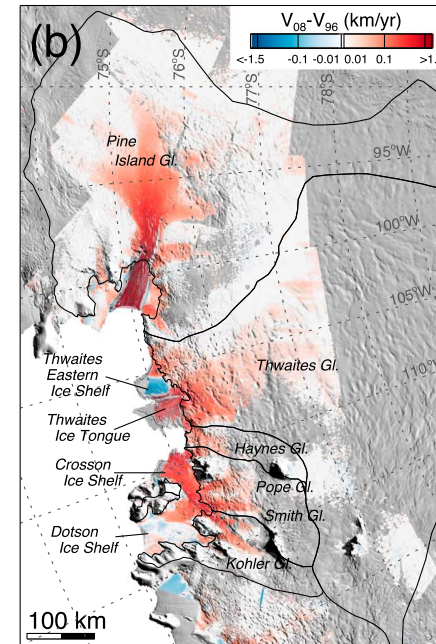


# Ice sheet collapse?

Marginal ice has accelerated and thinned over the last decade



McMillan et al 2014



Mouginot et al 2014

**Marine Ice Sheet Collapse Potentially Under Way for the Thwaites Glacier Basin, West Antarctica**

Ian Joughin, Benjamin E. Smith, Brooke Medley

**Collapse of the West Antarctic Ice Sheet after local destabilization of the Amundsen Basin**

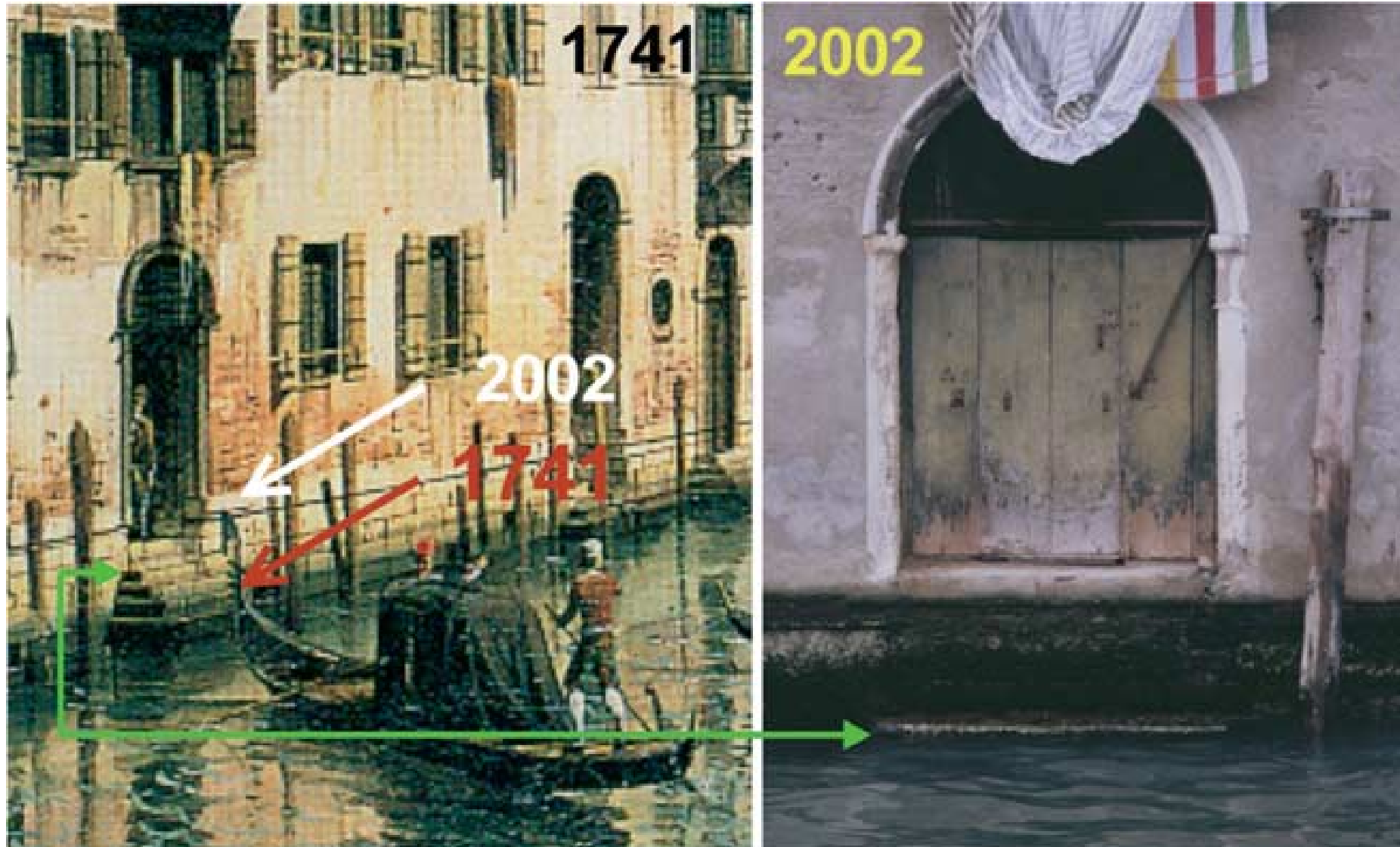
Johannes Feldmann<sup>a,b</sup> and Anders Levermann<sup>a,b,1</sup>

**When and why does rapid sea level change occur?**

**Can we constrain how fast it might happen?**

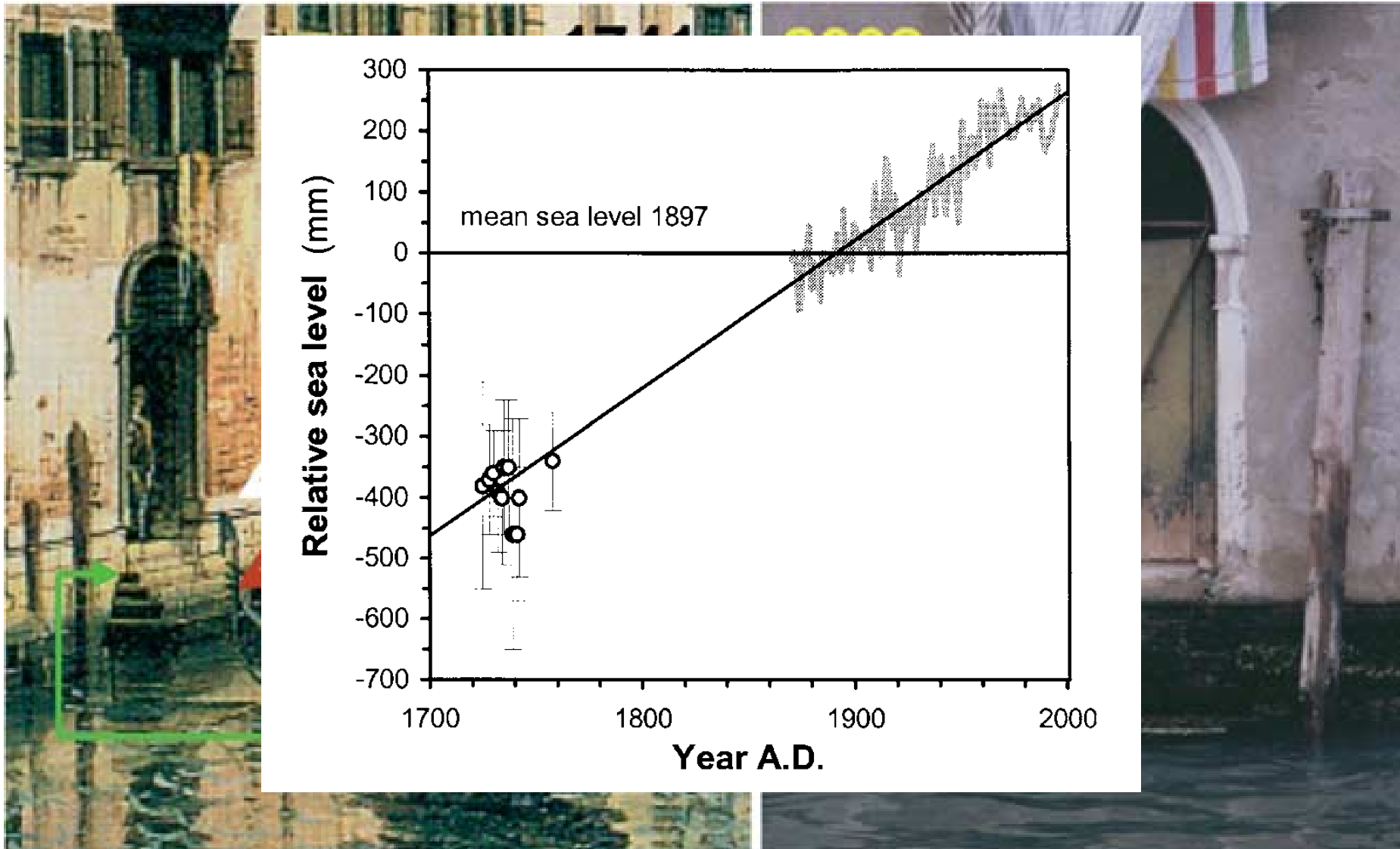
# Sea level rise

Venetian paintings by Canaletto & Bellotto

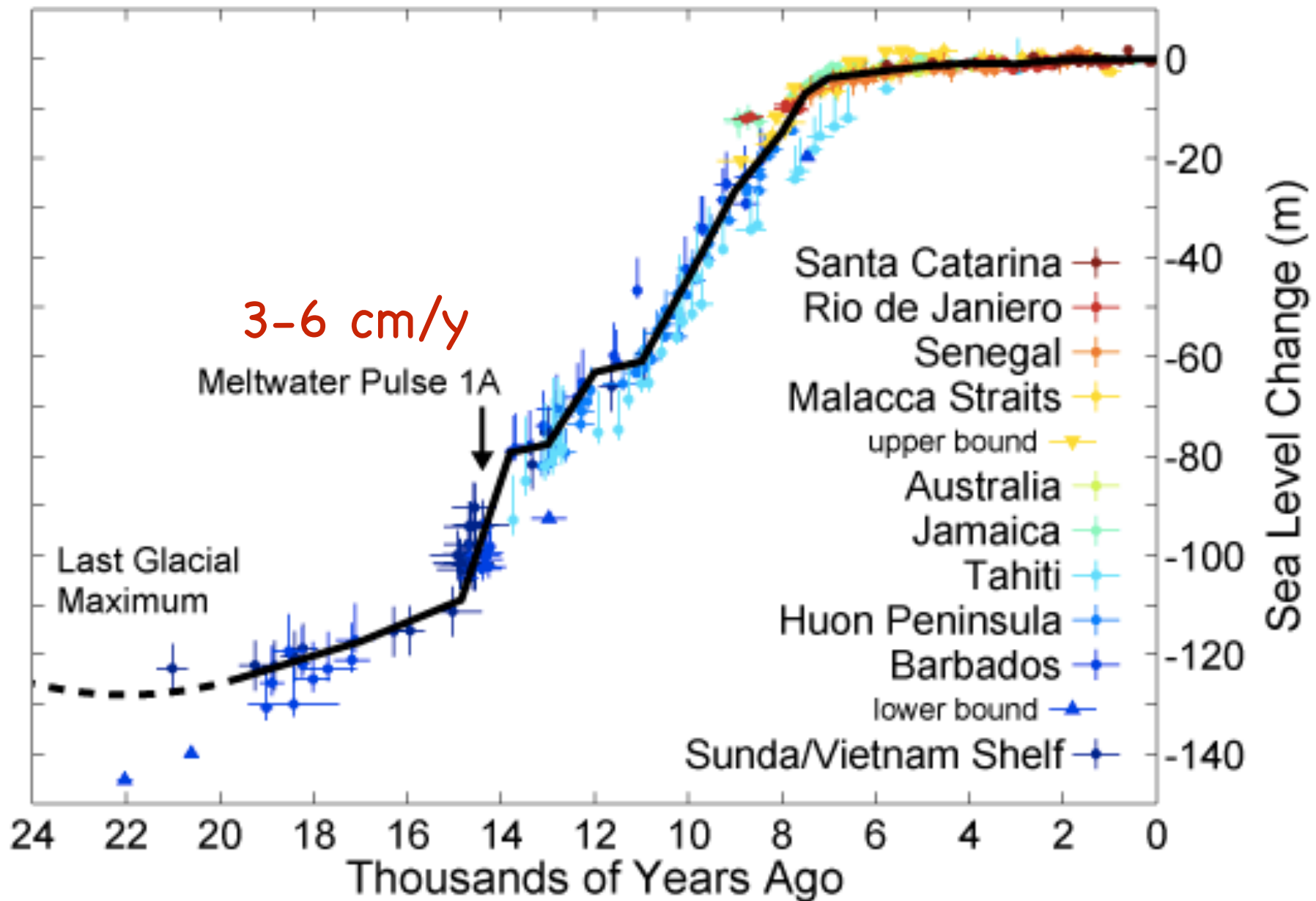


# Sea level rise

## Venetian paintings by Canaletto & Bellotto

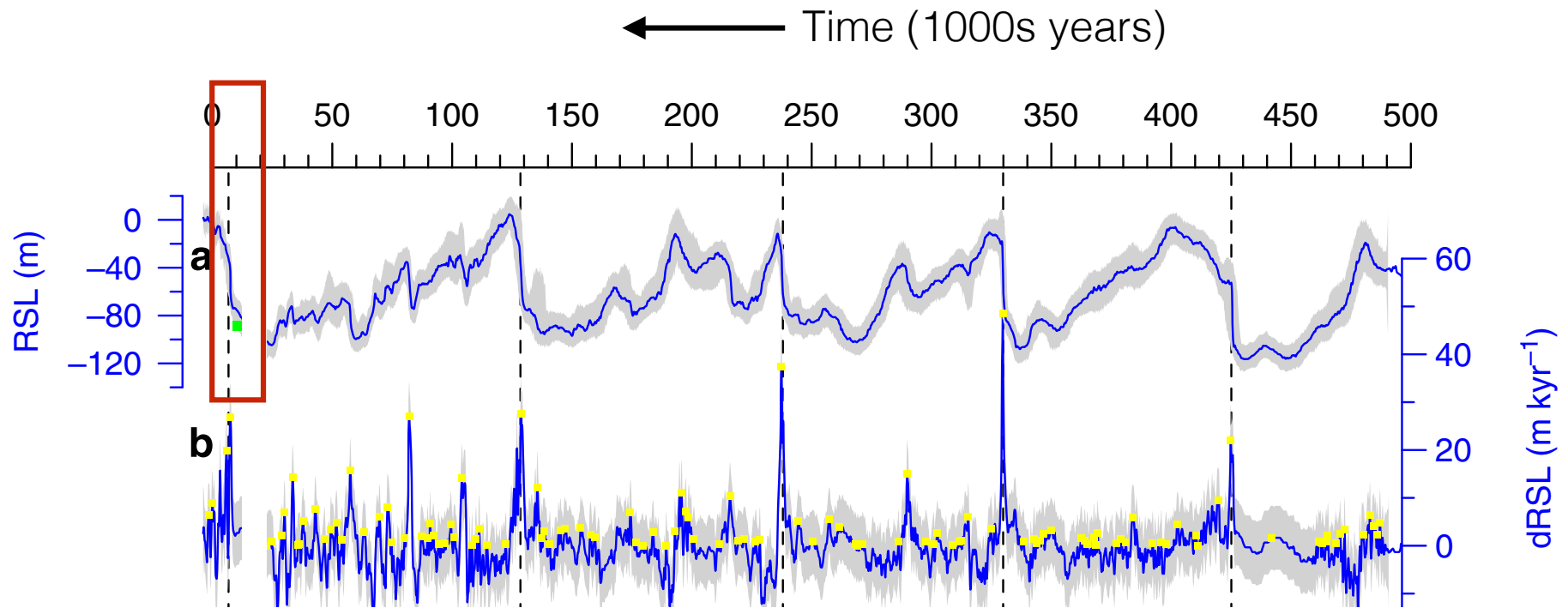


# Historical sea level



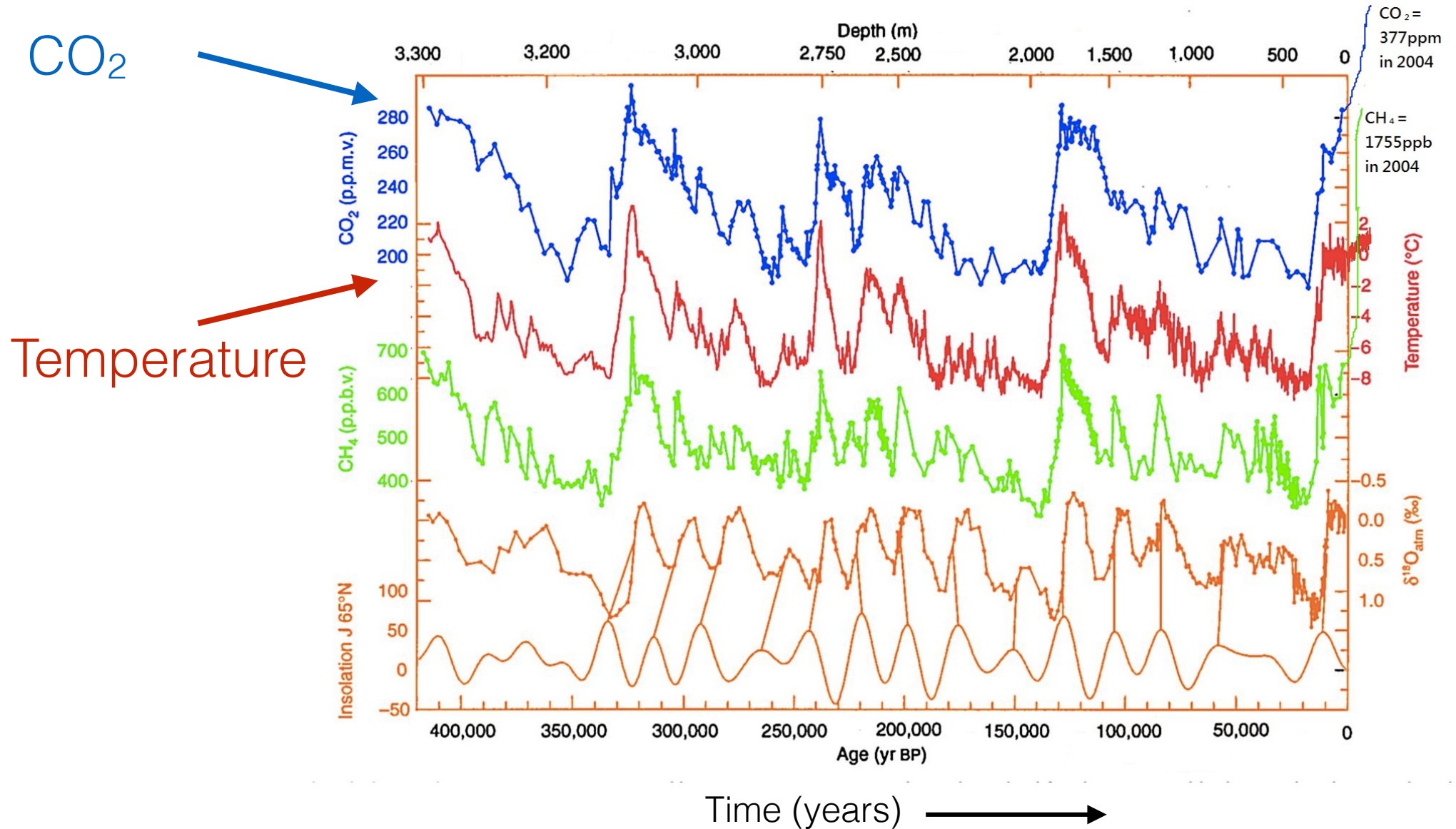
# Historical sea level

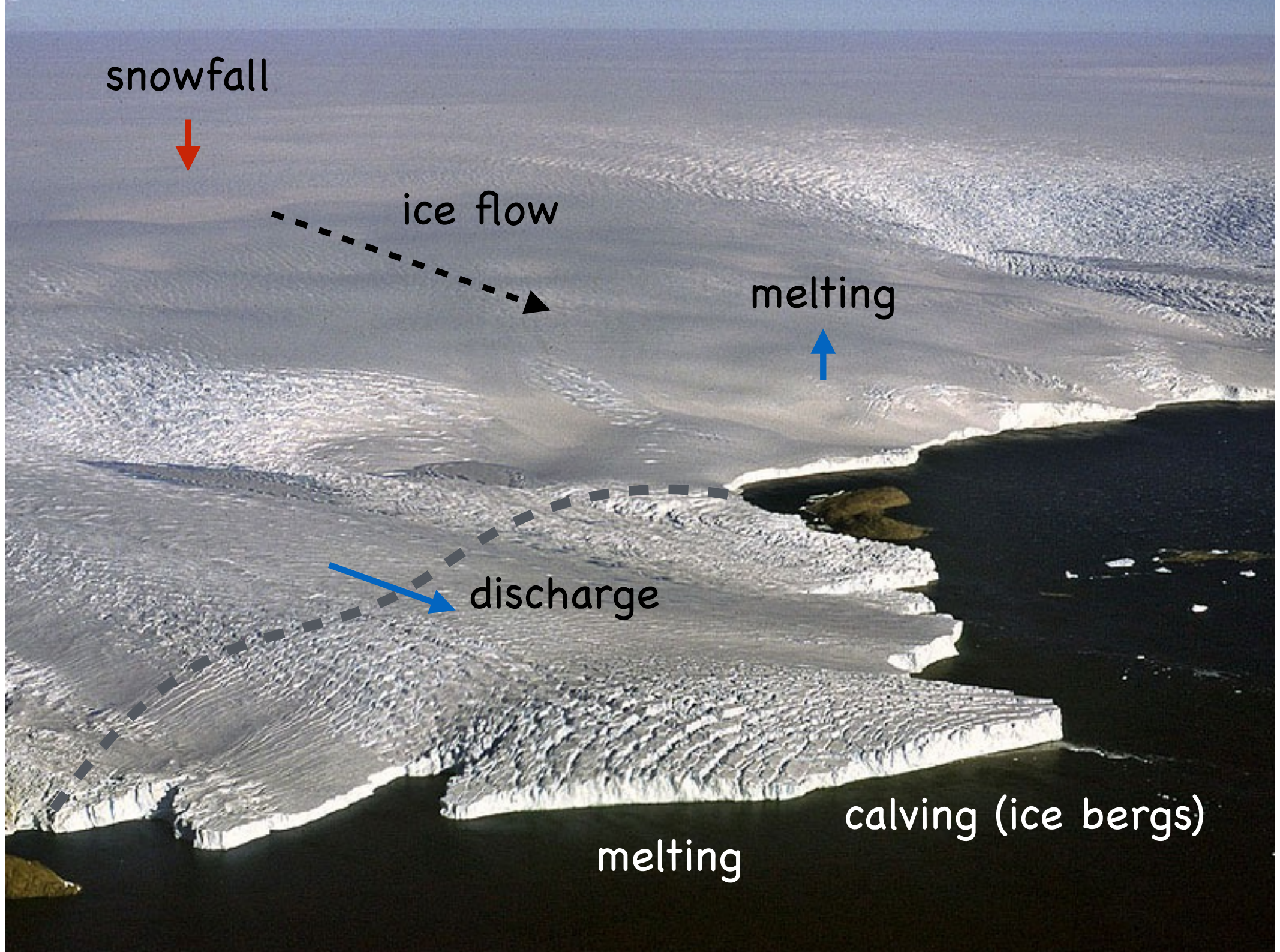
The glacial period is punctuated by several periods of rapid sea level rise  $> 1$  cm/y.



Grant et al 2014

# Antarctic ice core measurements





snowfall



ice flow



melting



discharge



calving (ice bergs)

melting

# A mathematical model

ice volume



$$\frac{dV}{dt} = A - M - Q$$

discharge



melting

accumulation (snow fall)

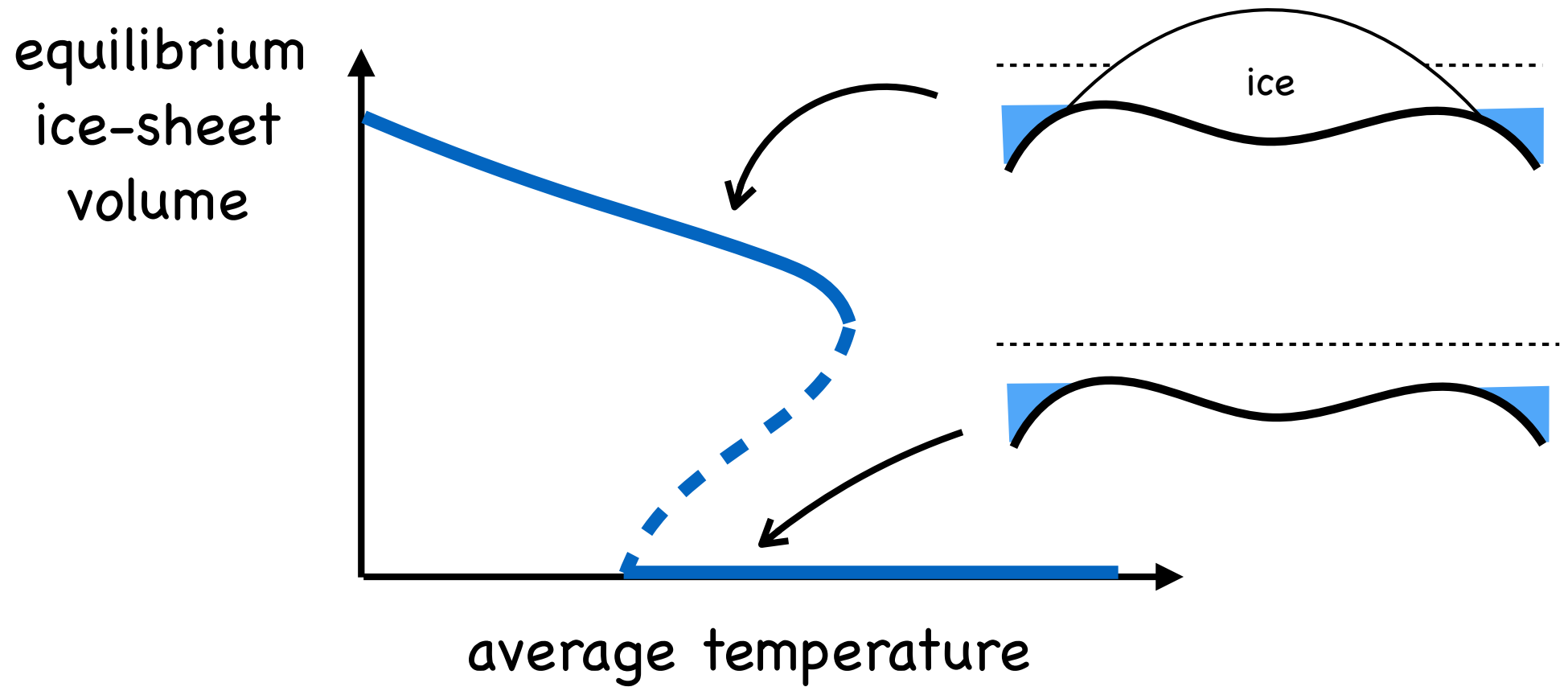


© 2015 James Balog

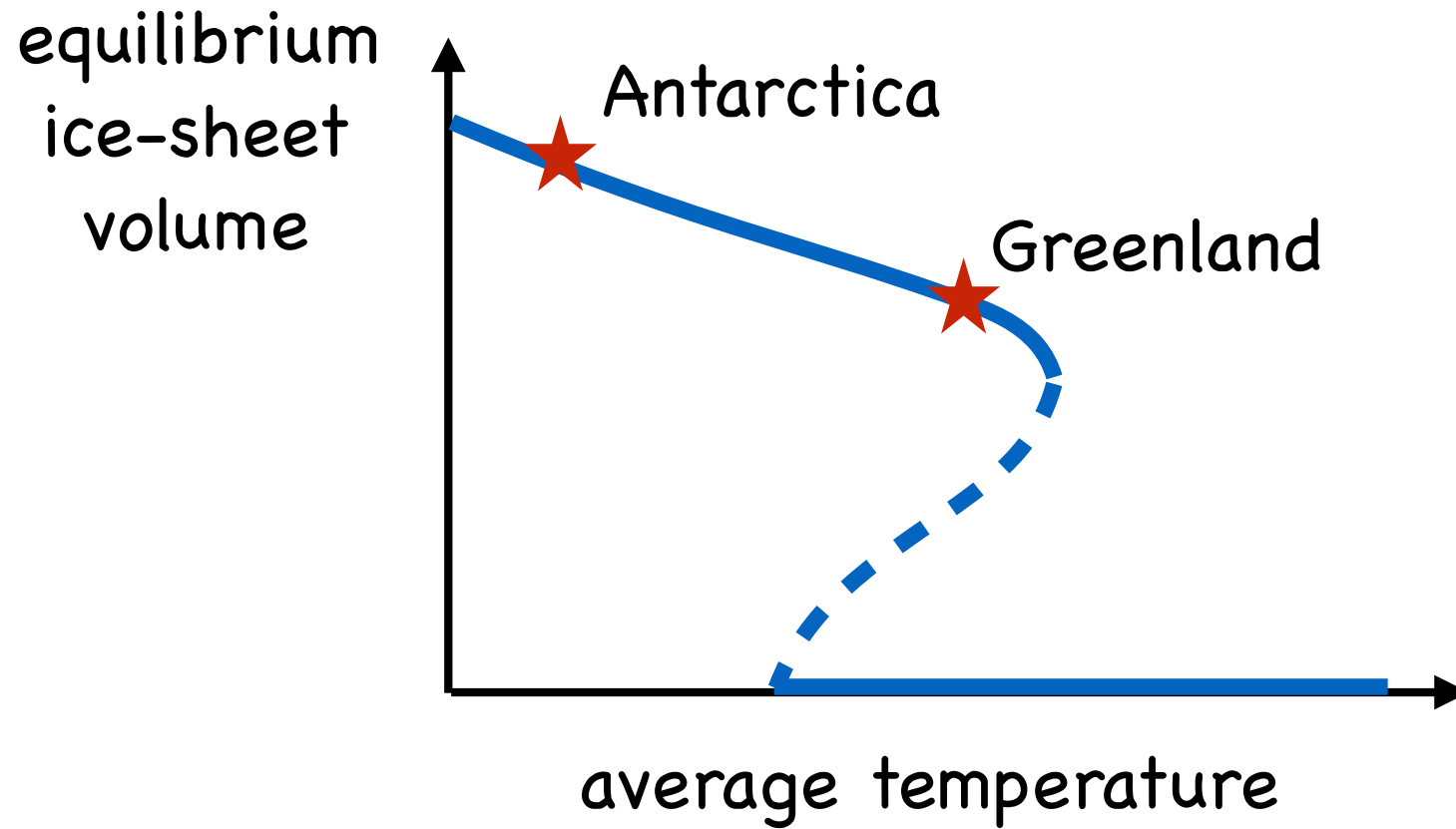
Extreme Ice Survey - Time-lapse camera  
Columbia Glacier, Alaska

# Ice-sheet elevation feedback - hysteresis

A higher ice surface leads to less melting

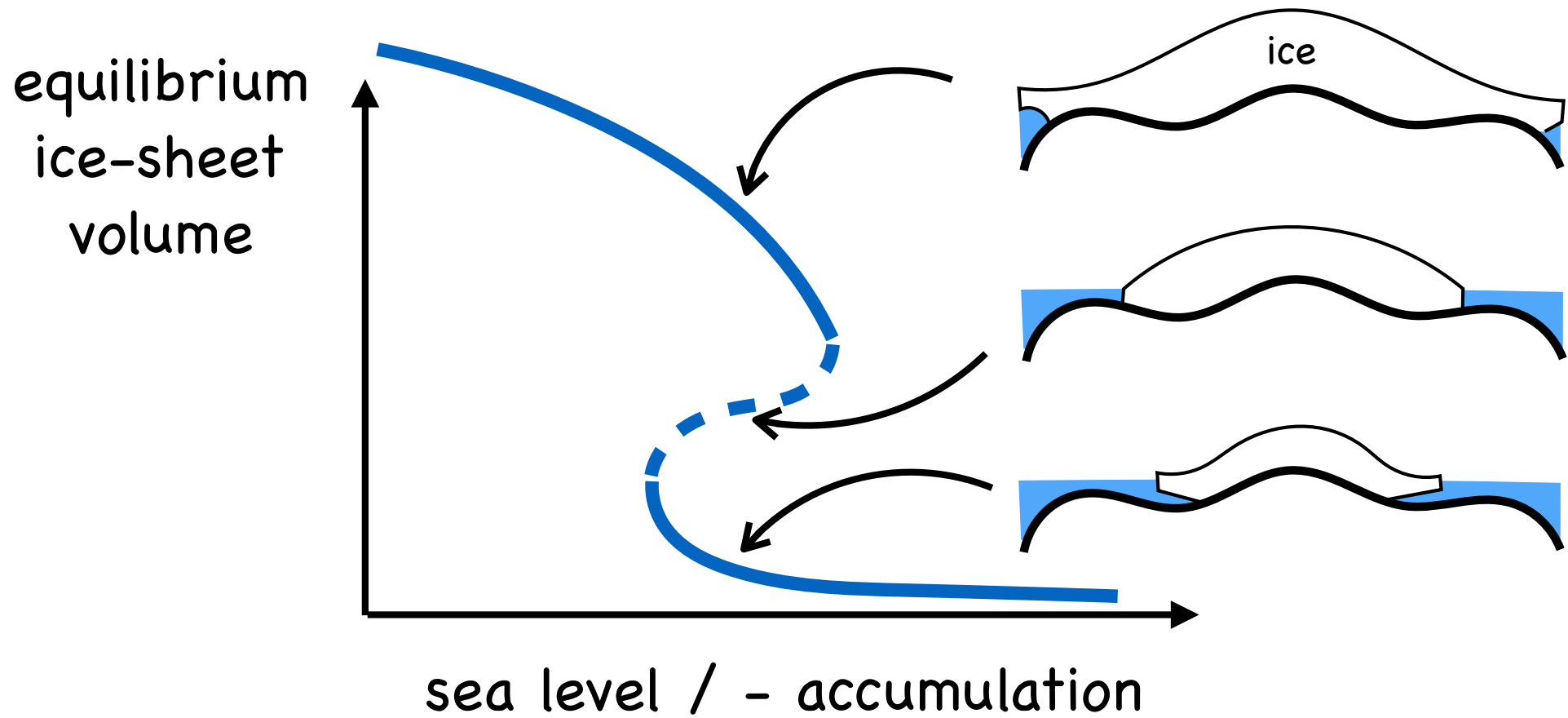


# Ice-sheet elevation feedback - hysteresis

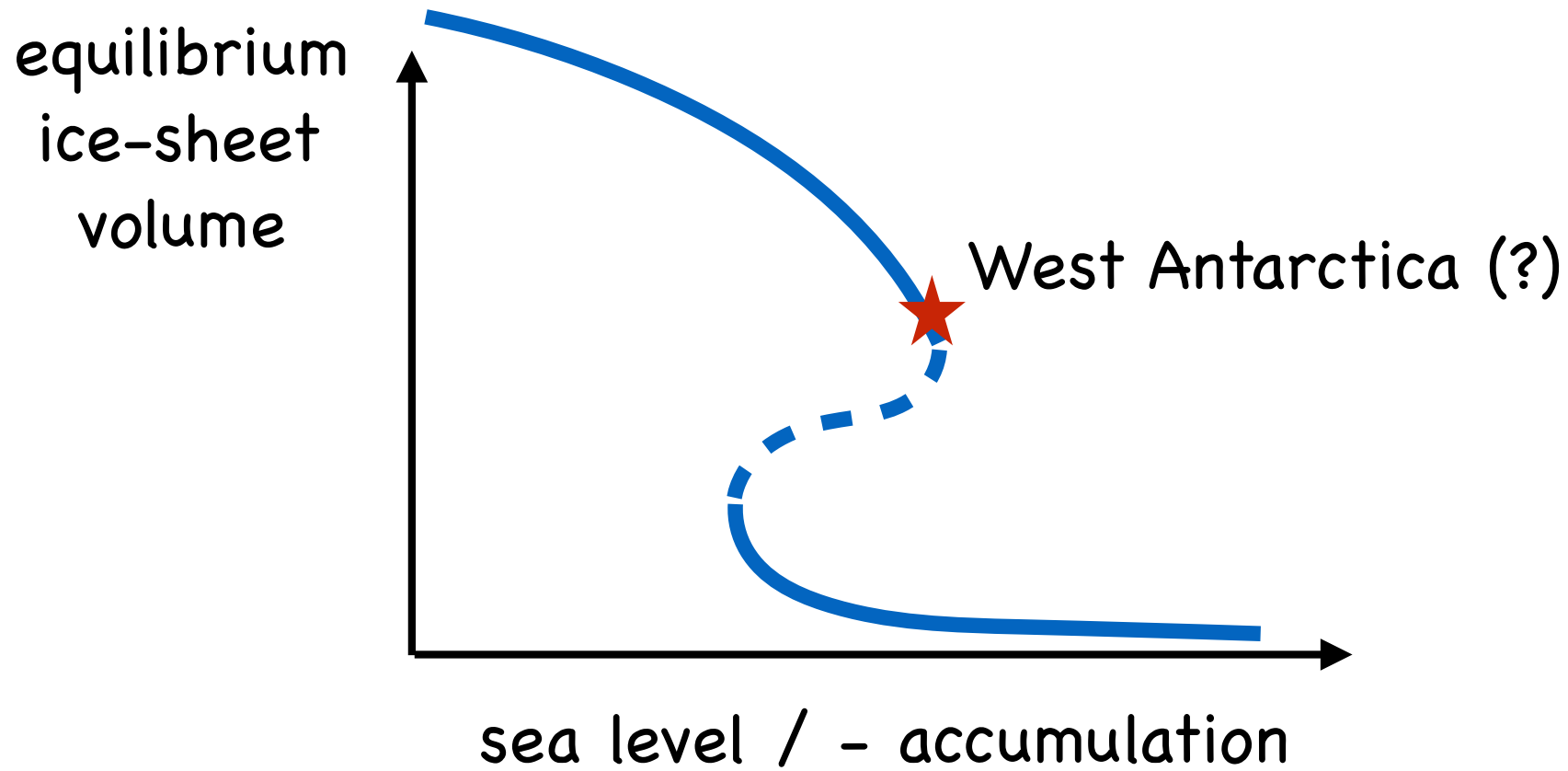


# Marine ice sheet instability

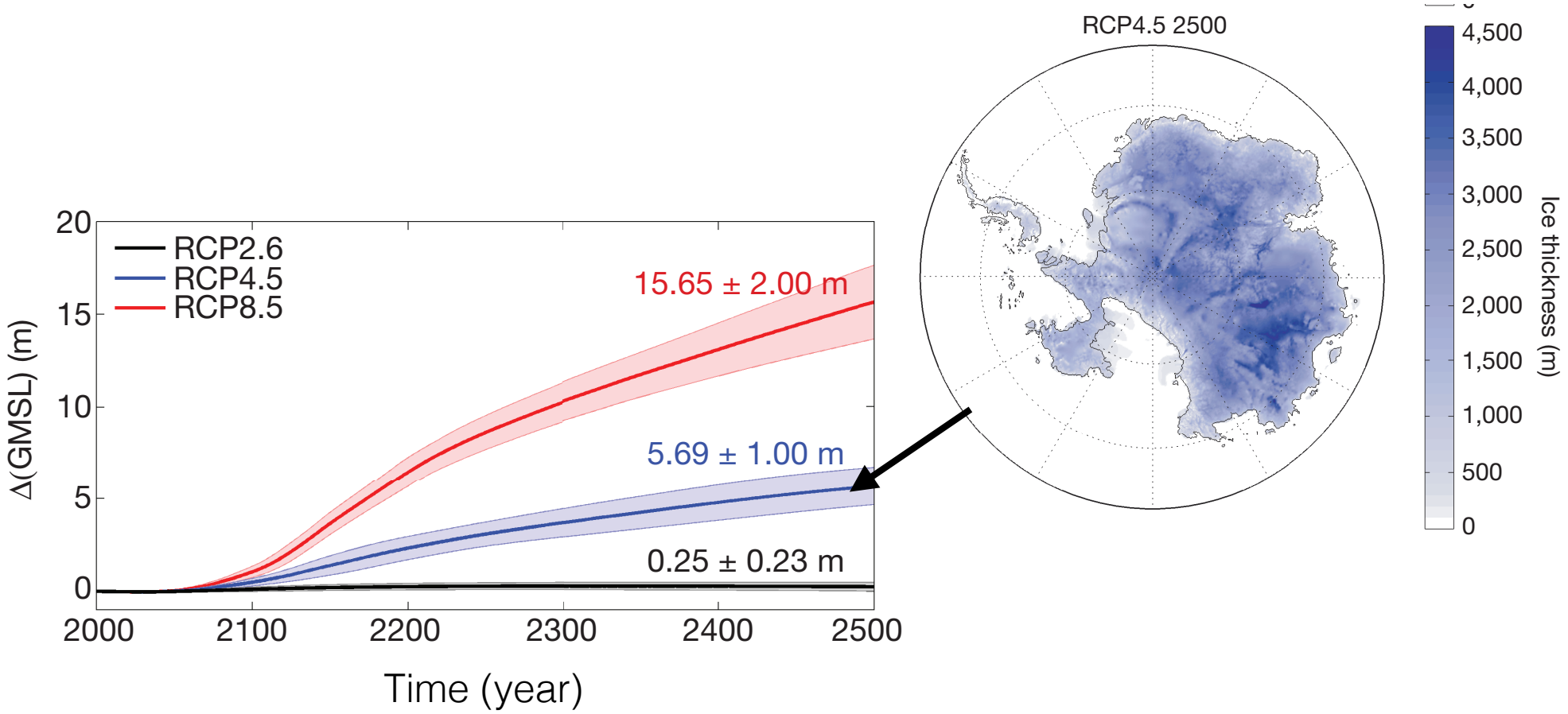
Deeper ocean at margin leads to larger ice flux



# Marine ice sheet instability



# Numerical models

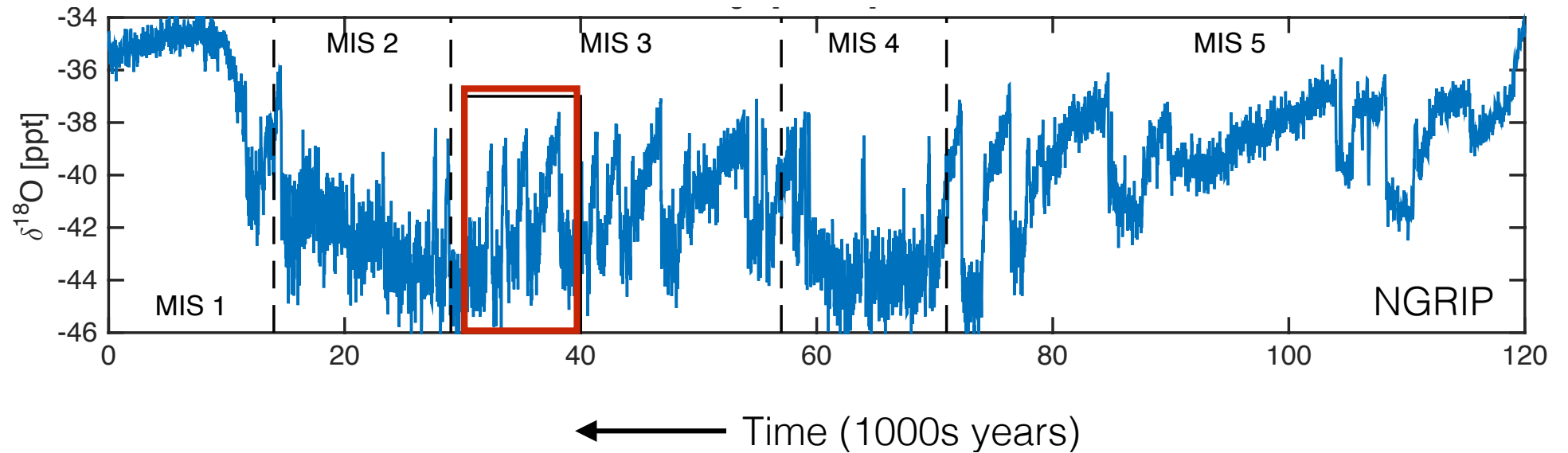


DeConto & Pollard 2016

**What drives historic climate change?**

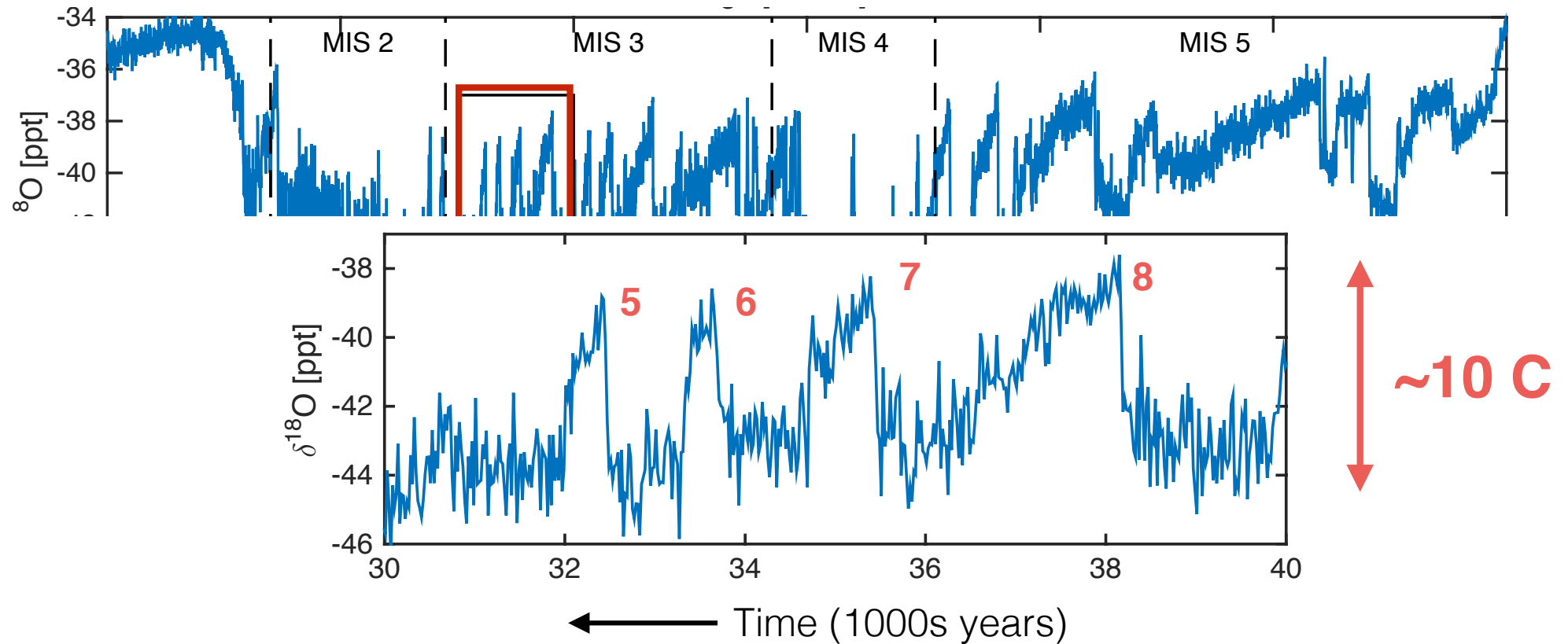
# Greenland ice core measurements

Oxygen isotopes are a proxy for past temperature.



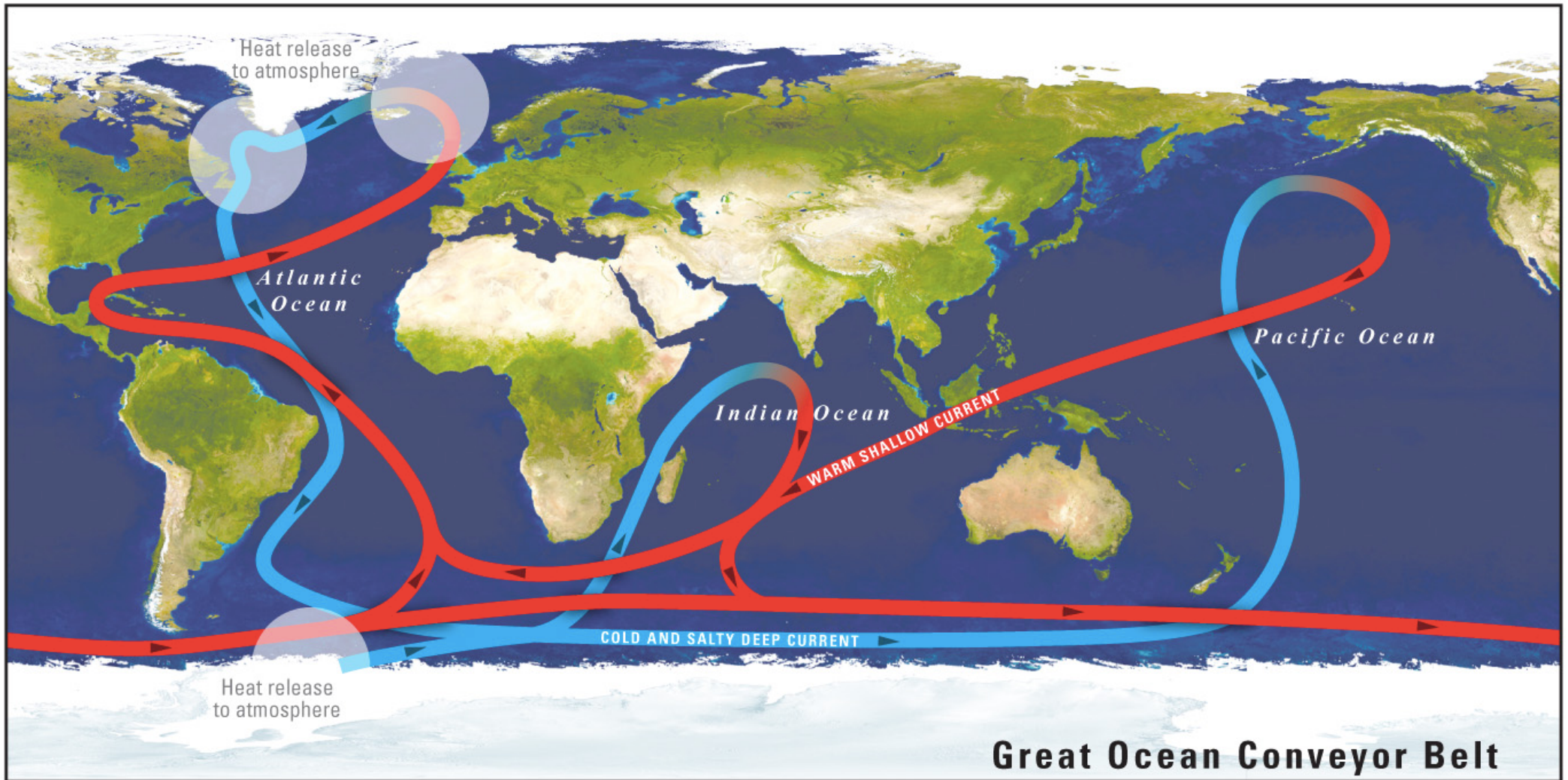
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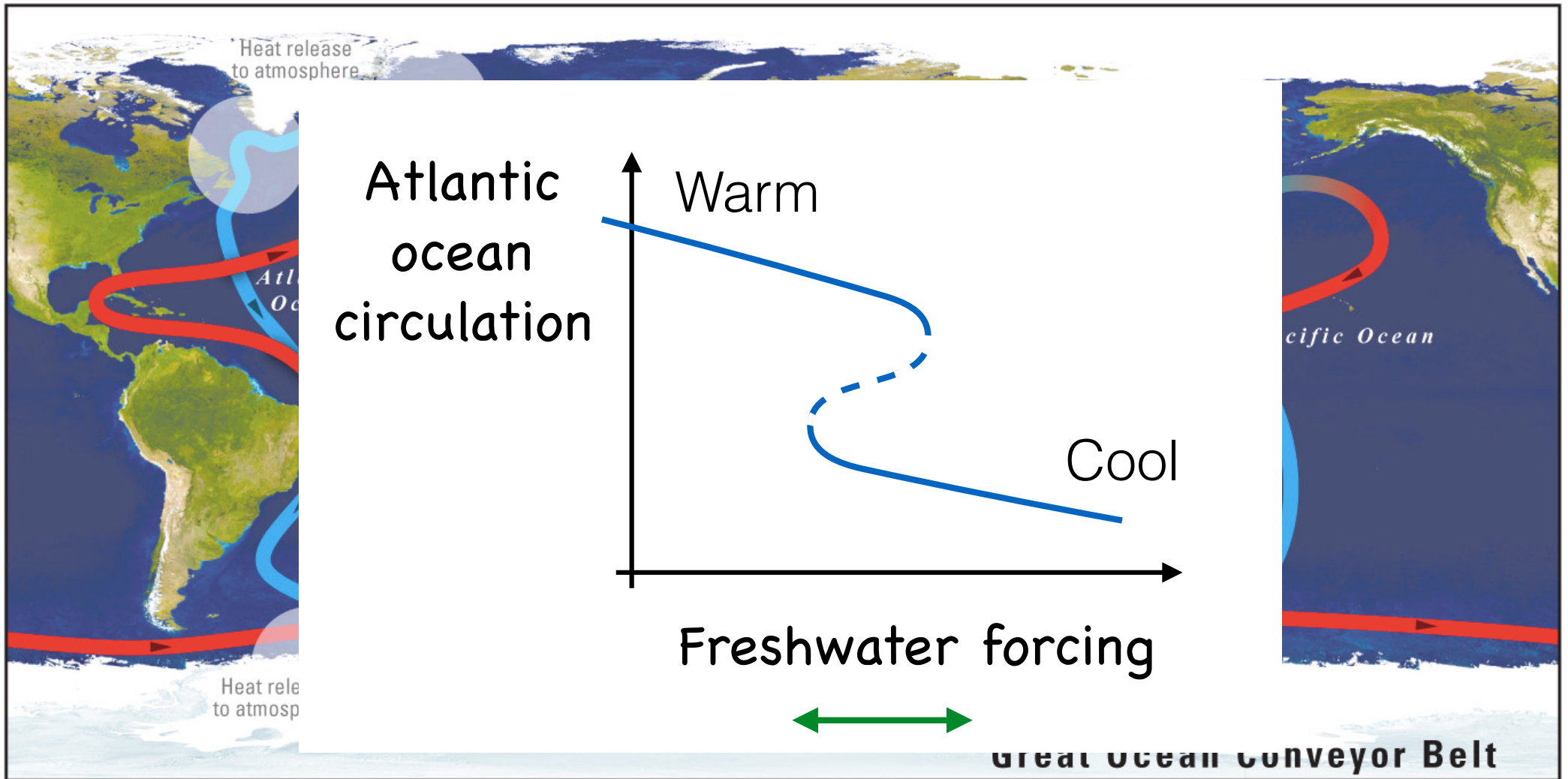
**Dansgaard-Oeschger** events:  $\approx 10\text{C}$  warming in  $< 50$  years

# Ocean circulation



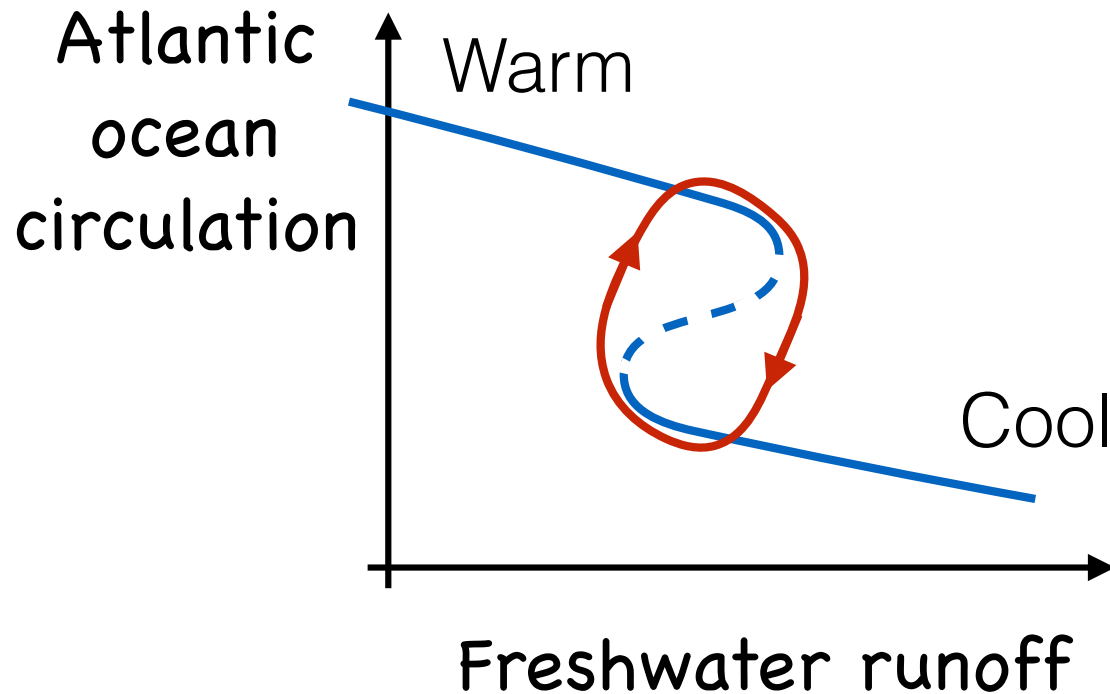
USGS

# Ocean circulation



# Relaxation oscillator

Runoff from NH ice sheets drives changes in circulation



*in review*, with Eric Wolff, Helen Johnson, Andrew Fowler, and others



thank you