



# Problems, Progress and Perspectives in Mathematical and Computational Biology

Qixuan Wang<sup>1,2</sup>  · Hans G Othmer<sup>3</sup> · Philip K Maini<sup>4</sup>

Received: 13 February 2026 / Accepted: 17 February 2026

© The Author(s), under exclusive licence to the Society for Mathematical Biology 2026

## Abstract

For this Special Collection we invited experts in the area of mathematical and computational biology to share their views on the major problems in their areas of interest and their recent research results – focusing on the development of state-of-the-art modeling approaches and computational techniques applied to problems in the life sciences – and to present their vision of the new directions needed for addressing unsolved problems. Papers in this Special Collection address mathematical and computational problems in several areas of the life sciences, including theoretical neuroscience, cancer modeling, and cell and developmental systems. With respect to methodologies, these papers cover dynamical systems, differential equations, stochastic processes, and modern computational techniques, all with an emphasis on techniques in modern modeling and computational methodologies. This Special Collection is jointly hosted by the Bulletin of Mathematical Biology and the Journal of Mathematical Biology.

**Keywords** Mathematical biology · computational biology

---

Qixuan Wang, Hans G. Othmer and Philip K. Maini have contributed equally to this work.

---

✉ Qixuan Wang  
qixuanw@ucr.edu

Hans G Othmer  
othmer@umn.edu

Philip K Maini  
Philip.Maini@maths.ox.ac.uk

<sup>1</sup> Department of Mathematics, University of California, Riverside, Riverside, California, USA

<sup>2</sup> Interdisciplinary center for data-driven modeling in biology, University of California, Riverside, Riverside, California, USA

<sup>3</sup> School of Mathematics, University of Minnesota, Twin Cities, Minneapolis, Minnesota, USA

<sup>4</sup> Wolfson Centre for Mathematical Biology, Mathematical Institute, University of Oxford, Oxford, United Kingdom

## 1 Introduction

During the past several decades, the scientific community has witnessed rapid development and advances both in experimental techniques in biology, and in mathematical modeling and computational techniques. Development of new experimental techniques creates a new world in the life sciences that researchers have not previously been able to access. New modeling concepts and methodologies are emerging to meet the increasing need from modern biology. For this Special Collection "Problems, Progress and Perspectives in Mathematical and Computational Biology", we invited seventeen contributions. They cover a broad range of topics in modern modeling research with applications in the life sciences, using various state-of-the-art modeling and computational methodologies to tackle problems across a range of systems: neuroscience, cell and development systems, and human diseases.

Mathematical oncology, or cancer modeling, remains one of the largest modeling research areas. Nowadays cancer modeling research spans the whole range from mechanistic modeling to data-driven statistical and machine learning approaches, aiming to explore both cancer development mechanisms and treatment of cancer dynamics as well as predict cancer growth based on knowledge of present and past data. One major question in general mechanistic modeling – including cancer growth modeling – concerns the interaction and integration of biochemical and biomechanical cues. To address this, a thermodynamically-consistent continuum model of growth-elasticity is used to investigate the chemo-mechanical regulation of tumor growth in Olanant et al. (2025). In addition to exploring cancer growth mechanisms, mechanistic models are also used to optimize cancer treatment. In recent years, virotherapy has become an emerging and promising cancer therapy. In Baabdulla and Hillen (2024), a combination of numerical analysis and bifurcation analysis is used to study the spatio-temporal virus infection pattern formation dynamics, leading to the minimal speed of travelling invasion waves for the cancer and the oncolytic viruses. In Brennan et al. (2025), the importance of spatial-patterning mechanisms in cancer development, as well as in treatment design and dosing optimization, is highlighted for the case of cancer immunotherapy. In Pasetto et al. (2024), a novel approach is proposed to estimate the patient-specific tumor carrying capacity, based on the logistic growth model.

Neurodegenerative diseases, including Alzheimer's disease, have a serious impact on many people. Therefore, theoretical neuroscience modeling has become an emerging and rapidly developing field. In Brennan and Goriely (2025) it is suggested that brain-scale network aggregation dynamics of prion-like neurodegenerative protein may contribute to drug design aimed at preventing whole-brain Alzheimer's disease progression. In the theoretical study of neuronal dynamics, modeling frameworks on both the micro- and network-scale are developed to explore the effects of heterogeneity in synaptic ensheathment on synaptic communication and network dynamics (Garcia et al. 2025).

Apart from disease modeling, cell and developmental biology remains a leading research area in theoretical biology. It ranges from cell fate dynamics, to tissue growth, and includes the general study of reaction-diffusion dynamics. Cell fate determination has been a major research focus in mathematical biology during the past few decades, deeply rooted in Waddington's epigenetic landscape theory. A random dynamical

system framework is presented in Vittadello et al. (2025), together with a tutorial outlining the current perspectives on cell fate. In development, domain establishment remains a classic open problem. In Stotsky and Othmer (2025), a comparison between pattern formation based on diffusion-driven transport vs. cytoneme-regulated transport is made, and the effect of their joint expression is investigated. Analytical results are derived for simple systems, while numerical results are provided for more complex systems. Another type of problem arises in cell biology, where many processes can be modeled using a reaction-diffusion system in a bounded domain (the cell membrane, cytoplasm, etc.), containing a set of small subdomains or interior compartments (such as membrane protein clusters, biological condensates, etc.). Such modeling problems are commonly referred to as singularly-perturbed diffusion problems. Bressloff (2024) presents a review of matched asymptotic analysis and Green's function methods to solve a general type of singular boundary value problem in 2D and 3D, where an inhomogeneous Robin condition is imposed on interior domain boundaries. In another theoretical study, Craciun and Erban (2025) investigate the existence and construction of multiple limit cycles in planar chemical reaction systems, with both algebraic and non-algebraic limit cycles considered.

On the methodology side, we received contributions based on various computational methods, including Boolean networks, agent-based modeling, stochastic modeling, and structured partial differential equation modeling. In addition, some authors have used state-of-the-art topological data analysis as a modeling technique. In each case these papers may serve as tutorials for the community, and provide insights on further development and extension of the methods.

In systems biology, Boolean networks have been widely used for modeling dynamical problems, including cell fate decisions and biological phenotypes. A recent question that arose in Boolean networks studies is the role of motif-avoidant attractors (MAAs). In Pastva et al. (2025) the authors present a review of the current state of knowledge on MAAs, together with novel insights on their regulatory roles. In addition, a large-scale computation of published Boolean models of biological systems verifies the rarity of MAAs in biological systems.

Agent-based models (ABMs) have been widely used for modeling complex biological and biomedical systems, due to their effectiveness in showing how individual behaviors at the microscale level give rise to emergent behaviors at the macroscale level. However, the high computational costs remain a barrier for parameter exploration, sensitivity analysis and uncertainty quantification. In recent years, ABM-based surrogate models have become a powerful tool to assist in analyzing the original ABM. A review of the most widely-used ABM surrogate modeling approaches, including statistical, mechanistic, and machine-learning-based approaches, as well as emerging hybrid approaches, is presented in Norton et al. (2026).

Stochastic simulation has been a popular approach to explore various stochastic dynamics, including reaction-diffusion processes. One major question is how to choose the size of the compartments used in stochastic reaction-diffusion modeling. A multi-grid reaction-diffusion master equation (mgRDME) is analyzed in Erban and Winkelmann (2025), where the grid sizes are allowed to vary across species, but remain constant for each species. Numerical simulations show that mgRDME models allow for high accuracy at reduced numerical cost.

In population dynamics, heterogeneity across individuals may result in dynamical behaviors that do not exist in an ideally-homogeneous population. In recent years, the contribution of phenotypic diversity to population dynamics has been acknowledged. Lorenzi et al. (2025) serves as a review of, as well as a tutorial on, phenotype-structured partial differential equation (PS-PDE) models, presenting standard tools and methods that can be used to derive, analyze, and numerically-compute solutions of PS-PDE models. In a theoretical study of phenotype-structured populations, focused on discretely-structured logistic growth models, necessary and sufficient conditions for exact moment closures are derived (Walker and Byrne 2025).

Topological data analysis (TDA) is an emerging field of computational mathematics that has been widely applied to biomedical research. While TDA has been widely used in data science over the past few years, this Special Collection contains two contributions that apply TDA to mechanistic modeling, shedding light on a promising future direction that integrates data science and mathematical modeling. In Yang et al. (2025), TDA is used to predict the occurrence of tumor niche formation surrounding blood vessels, by analyzing spatio-temporal data of cell locations generated from modeling synthetic data. Spector et al. (2026) illustrates an application of TDA to the study of pattern formation, using a topological clustering algorithm to reveal the dependence of pattern topology on parameters.

In summary, this Special Collection provides an overview of various modeling and computational methodologies, as well as example modeling systems. As is stated in the title, the contributions address the prevalent *Problems* in the various areas, present the most recent *Progress* toward addressing these problems, and incorporate useful *Perspectives* that hopefully provide a roadmap for future development in this field.

**Acknowledgements** Not applicable

**Author Contributions** Q Wang, H. G. Othmer and P. K. Maini contributed to the study, conception, design, manuscript writing and revision.

## Declarations

**Conflicts of interest** The authors have no conflict of interest to declare that are relevant to the content of this article.

**Open Access** This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit <http://creativecommons.org/licenses/by/4.0/>.

## References

Baabdulla AA, Hillen T (2024) Oscillations in a spatial oncolytic virus model. Bull Math Biol 86(8):93

- Brennan GS, Goriely A (2025) A network aggregation model for amyloid- $\beta$  dynamics and treatment of alzheimer's diseases at the brain scale. *J Math Biol* 90(2):22
- Brennan M, Krause AL, Villar-Sepúlveda E, Prior CB (2025) Pattern formation as a resilience mechanism in cancer immunotherapy. *Bull Math Biol* 87(8):1–31
- Bressloff PC (2024) Cellular diffusion processes in singularly perturbed domains. *J Math Biol* 89(6):58
- Craciun G, Erban R (2025) Planar chemical reaction systems with algebraic and non-algebraic limit cycles. *J Math Biol* 90(6):64
- Erban R, Winkelmann S (2025) Multi-grid reaction-diffusion master equation: applications to morphogen gradient modelling. *Bull Math Biol* 87(1):6
- Garcia N, Reitz S, Handy G (2025) Extending mathematical frameworks to investigate neuronal dynamics in the presence of microglial ensheathment. *Bull Math Biol* 87(5):1–32
- Lorenzi T, Painter KJ, Villa C (2025) Phenotype structuring in collective cell migration: a tutorial of mathematical models and methods. *J Math Biol* 90(6):61
- Norton K-A, Bergman D, Jain HV, Jackson T (2026) Advances in surrogate modeling for biological agent-based simulations: Trends, challenges, and future prospects. *J Math Biol* 92(1):6
- Olaranont N, Wei C, Lowengrub J, Wu M (2025) Chemomechanical regulation of growing tissues from a thermodynamically-consistent framework and its application to tumor spheroid growth. *J Math Biol* 91(3):31
- Pasetto S, Harshe I, Brady-Nicholls R, Gatenby RA, Enderling H (2024) Harnessing flex point symmetry to estimate logistic tumor population growth. *Bull Math Biol* 86(11):135
- Pastva S, Park KH, Huvar O, Rozum JC, Albert R (2025) An open problem: Why are motif-avoidant attractors so rare in asynchronous Boolean networks? *J Math Biol* 91(1):11
- Spector R, Harrington HA, Gaffney EA (2026) Persistent homology classifies parameter dependence of patterns in Turing systems. *Bull Math Biol* 88(1):10
- Stotsky J, Othmer HG (2025) The role of cytonemes and diffusive transport in the establishment of morphogen gradients. *Bull Math Biol* 87(2):21
- Vittadello ST, Diaz L, Liu Y, Zanca A, Stumpf MP (2025) Towards a mathematical framework for modelling cell fate dynamics. *J Math Biol* 91(5):1–43
- Walker BJ, Byrne HM (2025) On discretely structured growth models and their moments. *Bull Math Biol* 87(6):71
- Yang J, Fang H, Dhese J, Yoon IH, Bull JA, Byrne HM, Harrington HA, Grindstaff G (2025) Topological classification of tumour-immune interactions and dynamics. *J Math Biol* 91(3):25

**Publisher's Note** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.